



(BRIEF) SUMMARY

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Renormalization, regularization

Radiative corrections

Djangoh

TGEANTXTDJANGOH

RENORMALIZATION : WHAT IS IT ?

for effects in self-interactions. calculated quantities by altering the used to treat infinities coming from techniques in Quantum Field Theory Renormalization is a collection of values of these quantities to compensate

DIVERGENCE IN QED

30's : Discovery of divergence in perturbative calculations (Born, Heisenberg, Jordan, Dirac)

30's/40's : Descriptions of these divergences (e.g. virtual particle closed loop) (Stueckelberg, Schwinger, Feynman, Tomonaga, Dyson)

Virtual particles : obey E/p conservation but can be off-shell.

within the loop. If there's a loop, all variation of loop particle must be compensated

To find amplitude of the loop, one must integrate over all possible combinations !



UV DIVERGENCE	
The UV divergence is defined by :	
igtiestimes a region of integral with loop particles with high E/p	
short wavelength, high frequency in field states the second secon	
igstacless short proper time between emission and absorption	
There are three one-loop divergent loop diagrams :	
Vacuum polarization Self-energy Verte	ertex correction
The three divergences correspond to three parameters of the	the theory :
field normalisation Z	
mass of the electron	
charge of the electron	л

IR DIVERGENCE

The IR divergence is due to massless particles.

charged particles emits coherent photons with infinite wavelength

amplitude for emitting any finite nb of photon is null.

In this case, don't need to renormalize a parameter of the theory. Removal of IR divergence by including diagrams similar to vertex correction :



Can't tell difference between VC and Bremsstrahlung : both must be included.



SOME WORDS ON REGULARIZATION

Dealing with infinite and divergence is a tricky business.

For ex, what to do with some $\infty - \infty$ quantities ?

Answer : Regularization ! (ad-hoc proc.)

Ex:

$$V(r) = \frac{k}{r}$$
 Newton potentiel in sph. coordinates
Singularity in 0.
 $V_{\varepsilon}(r) = \frac{k}{\sqrt{r^2 + \varepsilon^2}}$ Introduction of family of one parameter

$$V_{\varepsilon}(0) = \frac{k}{\varepsilon} < +\infty$$
 Defined expression at $r = 0$

SOME WORDS ON REGULARIZATION

regulator in form of a cutoff such as integral converge. In QFT, modification on the boundaries of integration : introduction of

Putting cutoff to infinity recovers the original integral

cancellation, cutoff is put to infinity and physics results are recovered. With cutoff, infinite quantities goes finite and can cancel. After

Ex : Zeta function regularization

$$\zeta(s) = \sum_{n=1}^{\infty} n^{-s} = 1^{-s} + 2^{-s} + 3^{-s} + \dots \qquad analytic prolongation \qquad \zeta(-1) = -\frac{1}{12}$$

Similarly: $I(n,\Lambda) = \int_{0}^{\Lambda} p^{n} dp \sim 1 + 2^{n} + \dots + \Lambda^{n} \rightarrow \zeta(-n) \quad when \quad \Lambda \rightarrow \infty$

Improving this into an algorithm (Hartle, Garcia, Elizalde) :

$$I(n,\Lambda) = \frac{n}{2}I(n-1,\Lambda) + \zeta(-n) - \sum_{r=1}^{\infty} \frac{B_{2r}}{(2r)!} \frac{\Gamma(n+1)}{\Gamma(n-2r+2)} (n-2r+1)I(n-2r,\Lambda)$$

INTRODUCTION TO RADIATIVE CORRECTION

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When extracting PDFs or FFs, obtain cross-sections :

$$\boldsymbol{\tau}_{\mathrm{exp}} = \boldsymbol{\sigma}_{th} \left[F_n \left(\boldsymbol{x}, \boldsymbol{Q}^2, \ldots \right) \right]$$

Taking into account higher order corrections :

$$\boldsymbol{\sigma}_{th} = \boldsymbol{\sigma}^{(0)} [F_n] + \boldsymbol{\alpha}_{em} \boldsymbol{\sigma}^{(1)} [F_n] + \dots$$

Experimental problem :

can't distinguish radiative photon from non-radiative ones...



OBSERVED CROSS-SECTION

It is the convolution of the true cross-section times the radiator function :

$$\sigma^{obs}(p,q) = \int \frac{d^3k}{2k^0} R(l,l',k) d\sigma^{true}(p,-q,k)$$

Same goes for structure functions :

$$F_n^{obs}(x,Q^2) = \int d\tilde{x} \, d\tilde{Q}^2 R_n(x,Q^2,\tilde{x},\tilde{Q}^2) F_n^{true}(\tilde{x},\tilde{Q}^2)$$

Formulas can be extended for higher-order multi-photon emission.

UNFOLDING
Determination of the true cross-sections from the measured ones :

$$d\sigma^{obs}(p,q) = \int \frac{d^3k}{2k^0} R(l,l',k) d\sigma^{true}(p,-q,k)$$

Typical answer : an iterative solution !
But, ill defined : \geq no unique solution
 \geq large uncertainties
 \geq numerically unstable
However, with partial functioning : $R(l,l',k) = \frac{I}{k \cdot l} + \frac{F}{\dot{Q}^2} + \frac{C}{\dot{Q}^2}$
 \geq Initial state radiation : k.l small for $\ll (l_m, \gamma) \rightarrow 0$
 \geq Final state radiation : k.l' small for $\ll (l_m, \gamma) \rightarrow 0$
 \geq Compton peak : Q² small for $p_r(l_m) - p_r(\gamma)$

SOME REMARKS ON LEPTONIC RADIATION

 $E_{\gamma,\max}^2 \propto Q^2 \frac{1-x}{x}$ X

- Large radiation at large Q²-small x
- Radiation suppressed at small Q²-large x
- Large negative correction from

unconcealed virtual contribution

 $\tilde{Q}_{\min}^2 \propto \frac{x^2}{1-x} M_N^2$

 $\widetilde{Q}^2 \ll \widetilde{Q}^2$ possible

SOME WORDS ON HADRONIC RADIATION

Cancels with loops, collinear emission give rise to correction of type :

$$\frac{\alpha}{2\pi} \log \left[m_q^2 \right] \quad \text{where} \quad m_q = 0$$

Solution is to factorize and absorb the divergences into PDF.

$$d\sigma = \sum_{f} d\hat{\sigma}_{f} \left[1 + \delta_{f} \left(Q^{2}, m_{q}^{2} \right) \right] q_{f}(x) = \sum_{f} d\hat{\sigma}_{f} \hat{q}_{f}(x, Q^{2})$$

However, due to the difference of charge between quarks, there's an isospin violating effect







induces that eventually some hadrons fall into the wrong (x,y) bin Difference between the hadronic and leptonic kinematic variables

Applying the correction factor to multiplicities is indirectly 'redirecting' hadrons fallen in wrong (x,y) bins into the right ones





FINDING THE BEST RC GENERATOR



Can we use another MC generator for radiative events and see if it reproduces the results of RADGEN ?

DJANGOH

DJANGOH, concatenation of DJANGO and HERACLES :

- Event generator for neutral/charged current ep interactions at HERA by H. Spiesberger.
- Simulates DIS including both QED and QCD radiative effect.
- Includes single photon emission from lepton/quark line, self energy corrections and complete set of one-loop weak corrections
- Includes also the background from $ep
 ightarrow ep \gamma$.
- Capable of obtaining hadronic final state via the use of JETSET.
- Modified to work for µp interactions.
- Uses exact calculations and no approximations
- Fortran framework.

Energy distribution for radiated photon, outgoing muon and struck quark.



SELF-CONSISTENCY OF DJANGOH

SELF-CONSISTENCY OF DJANGOH



DJANGOH/RADGEN COMPARISON



DJANGOH produces more soft photons than hard photons First observation :



TGEANT

simulation for the COMPASS-II GEANT4-based Monte-Carlo

experiment.

Modular C++ framework

Can handle event generators for specific interaction simulation



WAYS TO IMPLEMENT A GENERATOR IN TGEANT

'Internal' generator

Pythia

HepGen++

- C++ Interface
- Perfect conservation of P(p,E)
- Need beamfile for primary generator in TGEANT

OR

'External' generator

- Lepto
- Beamfile read by standalone generator
- $igtilde{\mathbb{P}}$ Primary generation and process infos in one file
- P(p,E) not perfectly conserved (due to extrapolation to -9m..)



Conclusion : External implementation isn't fitted to Djangoh !	 At least 3 classes to implement Create a new file format to create the equivalent of the Lepto file for Djangoh Modify Djangoh so we can do backward propagation of the incoming µ Necessity to recover the output of LUJETS via a file Lot of access to file = Lot of computing time wasted 	Applicated to Djangoh :	EXTERNAL IMPLEMENTATION AND ITS PROBLEMS
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TGEANT : Beam Gen

TGEANT

C++ Interface to Djangoh recovers infos of Beamfile from TGEANT

Interface run Djangoh as subroutine

Interface send LUJETS result of Djangoh to TGEANT

Rotation of 4-V of outgoing particles

TGEANT creates outgoing particles, kill beam

DJANGOH

Recover results in detectors

TGEANT

INTERNAL IMPLEMENTATION OF DJANGOH

Number of classes needed : only 2 !

Interface Class : TDjangoh

- Is a standalone class (depends a bit from ROOT)
- Creates instance of Djangoh that can be manipulated in any C/C++ environment
- TDjangoh can be used within the ROOT framework (future use ?)

Process Class : T4DjangohProcess Do the I/O transfer of TGeant to TDjangoh Manipulates instance of TDjangoh Is a TGEANT class

INTERFACE CLASS

Changed input method of Djangoh :

- Standard method —→ input file.
- \gg But : input file is not efficient when producing 1M events changing input between each generation.
- Solution : drawing correspondence between struct in C++ and
- COMMON blocks in Fortran.
- Defined input values necessary for Djangoh in Interface

69	89	67	66	65	64	63	62	61	60
} ihscut_;-	<pre>float iwmin;-</pre>	<pre>float iymax;-</pre>	<pre>float iymin;-</pre>	<pre>float iq2max;-</pre>	<pre>float iq2min;-</pre>	• float ixmax;-	<pre>float ixmin;-</pre>	†	extern "C" struct ihscut

Corresponding COMMON block in Fortran

Struct in C++

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When a value is given to a member of the block in C++, we retrieve the same value in its Fortran counterpart and vice-versa.

INTERFACE CLASS

Output of Interface :

Lujets_t object containing the list of all particles.

- Lujets_t linked to LUJETS COMMON block.
- Can be obtained from Interface via GetLujets() method.
- ${igstrianglesize}$ Checked consistency between what obtained in Fortran subroutine and what recovered in Interface

20	19	18		16	15	14	13
÷	double	double	int	int	int	Ţ	struct
	V[5][4000];-	P[5][4000];-	K[5][4000];-	NPAD;	N;		Lujets_t∽

From Djangoh (fortran)

	16	5	14	13	12	11	10	9	ω	7	6	ຫ	4	ω	N	4	I	
	gamma	gamma	gamma	gamma	gamma	gamma	gamma	gamma	gamma	gamma	pi+	gamma	gamma	p+ IGEAN	<u>ج</u>	mu-	particle/jet	
sum:	1	4	4	4	4	4	1	1	4	1	1	4	4	1	4	4	ŝ	
0.00	22	22	22	22	22	22	22	22	22	22	211	22	22	2212	-321	13	ς Γ	Eve
	8	8	8	8	8	8	8	8	8	8	8	8	8	8	8	8	rig	nt li
-0.000	-8.892	0.014	0.001	0.137	-0.085	-0.116	-0.085	-0.050	-0.109	-0.105	-0.396	0.017	0.185	0.416	1.639	-1.371	p_×	sting (su
-0.000	0.033	0.111	-0.102	-0.068	0.158	0.203	0.082	0.348	0.114	-0.023	-0.119	-0.007	0.384	-0.413	0.142	-0.842	р_у	mmary)
160.000	0.416	0.353	0.916	1:079	1.452	3.625	1.170	3.881	2.146	1.058	4.098	0.170	7.085	0.512	17.036	115.003	p_z	
160.938	0.427	0.371	0.922	1.090	1.463	3.632	1.176	3.897	2.151	1.063	4.121	0.171	7.097	1.219	17.123	115.015	Coremits	
17.353	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.140	0.000	0.000	0.938	0.494	0.106	Netv	

From Interface

0.0427037 y : 0.281150 Q. 3.60494	acced installation of xercestan	; Generated !	UX INITIALIZED BY RLUXGO FROM SEEDS 2244 0	UX LUXURY LEVEL SET BY RLUXGO : 4 ¹¹⁸¹¹ P= 389 ⁰¹ OVCS ZUIIO	; Generation
			8		

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Results from Fortran subroutine are well passed to the Interface



OPTIM	IZING TDJAN	IGOH			
Djangoh ♥ to v ♥ to t	was designed vork with only hen run multip	: one input of in le event basec	coming leptor d on this uniqu	e energy e energy	
TGEANT	needs :				
w to	generate event means 1 event	s with incomir t = 1 energy	ng lepton ener	gy picked from	n beam file
The way	it is handled :				
No:	t really optimiz	ed : each time	, lot of redund:	ant stuff are m	ade
NOM	TGEANT	TGEANT	DJANGOH	TGEANT	
	Configure Djangoh with infos from setting file	Configure Djangoh with infos from beam file	Run Djangoh in its entirety	Recover result from Djangoh	
IDEAL	TGEANT	DJANGOH	TGEANT	DJANGOH	TGEANT
	Configure Djangoh with infos from setting file	Run initialisation subroutine once	Configure Djangoh with infos from beam file	Run event generation subroutine	Recover result from Djangoh 35

LOOKING FOR TIME CONSUMING PROCESSES

For 20 events

- Time elapsed : 4m 02s
- Means : 12.1 s/evt

Where does it take so long ?

Integration step where cross sections for radiative processes are calculated

Is it possible to do it once ? Integration step depends on the incoming particle energy, hence not trivial to do it once.

Look at 1 event

End	Event generation	Init user routine	Django6	Sampling	Integration/Init. for event sampling	Initialisation	
14	14	14	14	14	14	0	Total time elapsed (s)





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MODIFICATION OF DJANGOH Event generation step K-section calculation step nitialisation step to calculated X-sections for Generate events according corresponding X-sections Receive input from Interface radiative processes for radiative processes For one energy calculates E HSMAI Before

UBROUTINE HSINIT()

After

Receive input from Interface

For a GIVEN RANCE of energy calculates corresponding X-sections GRID for radiative processes

Generate events according to calculated X-sections for radiative processes picked in the GRID wrt. INPUT ENERGY

MODIFICATION OF DJANGOH

SUBROUTINE HSINIT()

Receive input from Interface

For a GIVEN RANGE of energy calculates corresponding X-sections

SUBROUTINE HSEVTG()

GRID for radiative processes

Generate events according to calculated X-sections for radiative processes picked in the GRID wrt. INPUT ENERGY

SUBROUTINE HSRCAP()

Do a sum-up of all generated events

- Overall : separate into subroutines and make sure subroutines are sharing correctly their infos
- HSINIT 1st part : Nothing special to do
- HSINIT 2nd part : Looping over integration for each step of the grid
- HSEVTG : Only modification is to pick the right entry in the grid according to input energy.
- HSRCAP : Do a recap of all generated events (% of RE, quark composition, etc.)





THE CROSS-SECTION GRID

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225 226 227 228 229 230 231 231 231 232 233 233 235 235 236 237 238	220 221 222 222 223 223 224
<pre>TYPE(xSection32) :: HSXN32- TYPE(xSection33) :: HSXN33- TYPE(xSection31C) :: HSXC31- TYPE(xSection32C) :: HSXC31- TYPE(xSection32C) :: HSXC32- TYPE(xSection32C) :: HSXC32- TYPE(xSection32C) :: HSXC32- TYPE(xSection32E) :: HSXE31- TYPE(xSection32E) :: HSXE32- HSXN22(100),HSXE32- HSXN31(100),HSXC2(100),HSXEL2(100),- HSXN31(100),HSXC2(100),HSXEL2(100),- HSXC31(100),HSXC32(100),HSXC33(100),- HSXC31(100),HSXC32(100),HSXC33(100),- HSXC31(100),HSXC32(100),HSXC33(100),- HSXC31(100),HSXE32(100),HSXC33(100),- HSXC31(100),HSXE32(100),HSXC33(100),-</pre>	<pre>C</pre>

Then declaration of COMMON Block that consists of tables of types

COMMON Block of GRIDS

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To initialize the grid, just loop over the different bins and take the center of the bin as energy of incoming lepton for c r o s s - s e c t i o n calculation.



EVENT GENERATION TIME IMPROVEMENT

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TDjangoh @ event generation :

10s before **0.1s** after (fact. 100)

TGEANTxTDjangoh @ event generation :

10-20s before 1-3s after (fact. 10)



Generation time improvement now limited by TGEANT



CONCLUSION

Renormalization and Radiative Corrections are often seen as complicated and black magic matters, but allow us to have precise results that sticks to the physics one wants to describe.

One can always recover the true crosssection from the one observed thanks to mathematical objects like radiators.

Thanks to these mathematical descriptions, possible to create event generators like Djangoh taking care of radiative events, allowing afterwards to calculate radiative corrections to apply to physical results.

As C/C++ is modular and versatile, possible -not without work !- to port Djangoh as a event generator for TGEANT.