

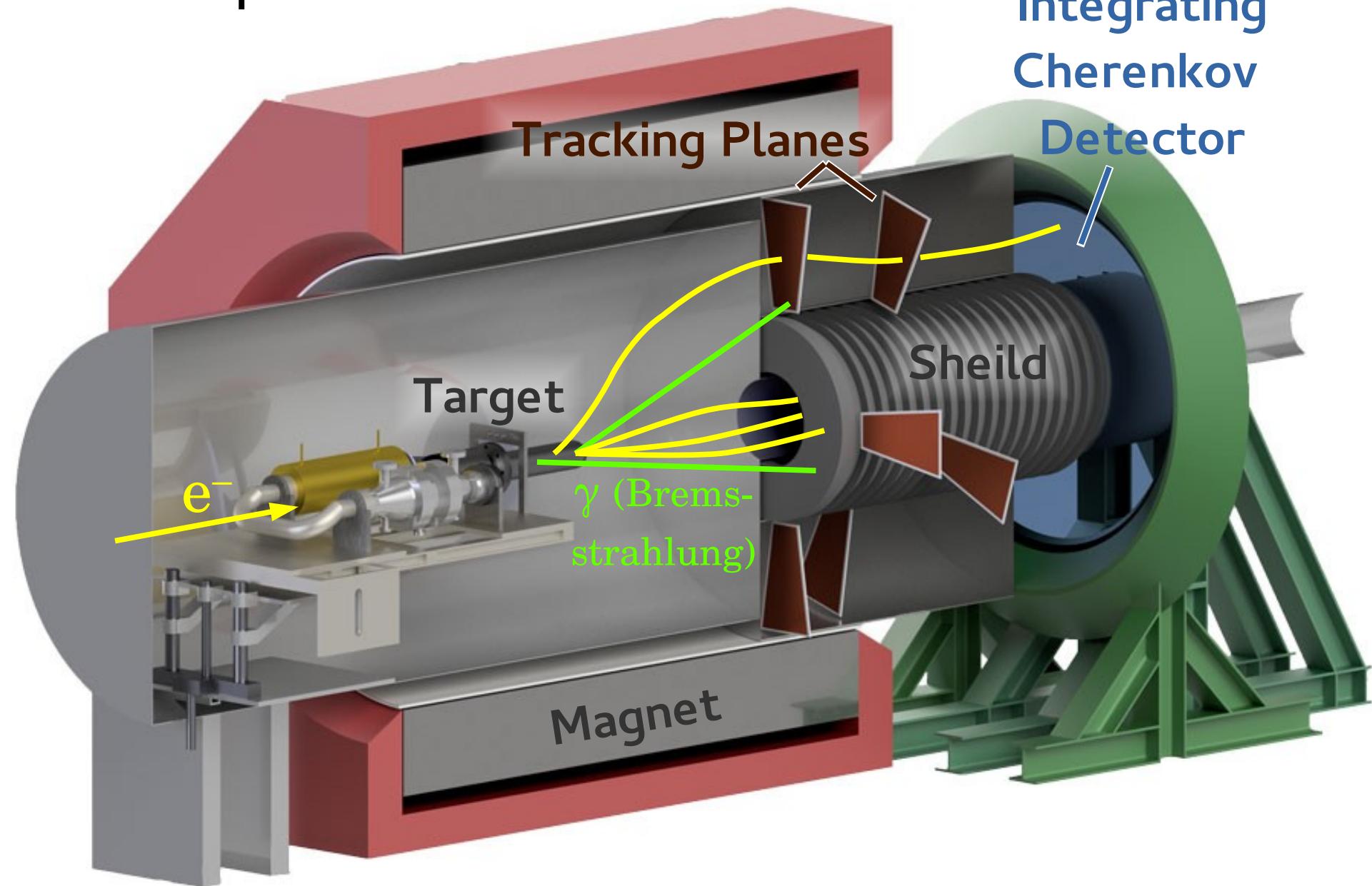


# Parameterization-based tracking for the P2 experiment

Iurii Sorokin

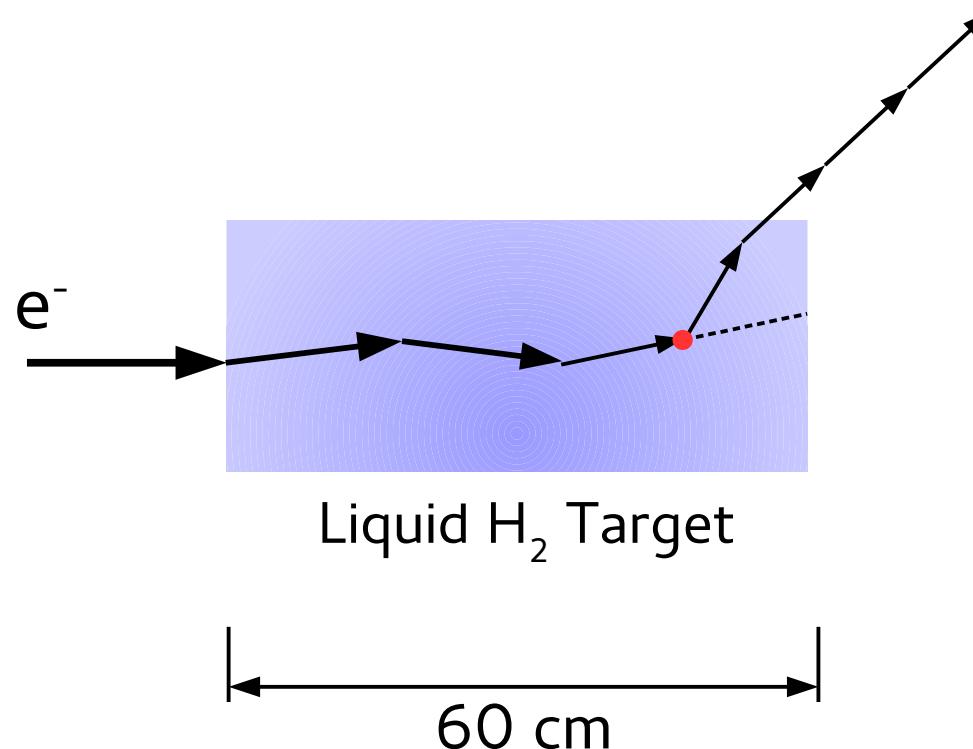
PRISMA Cluster of Excellence /  
Institute for Nuclear Physics, University of Mainz

# P2 setup



# Why is tracking necessary?

“Measure” actual  $Q^2$  distribution

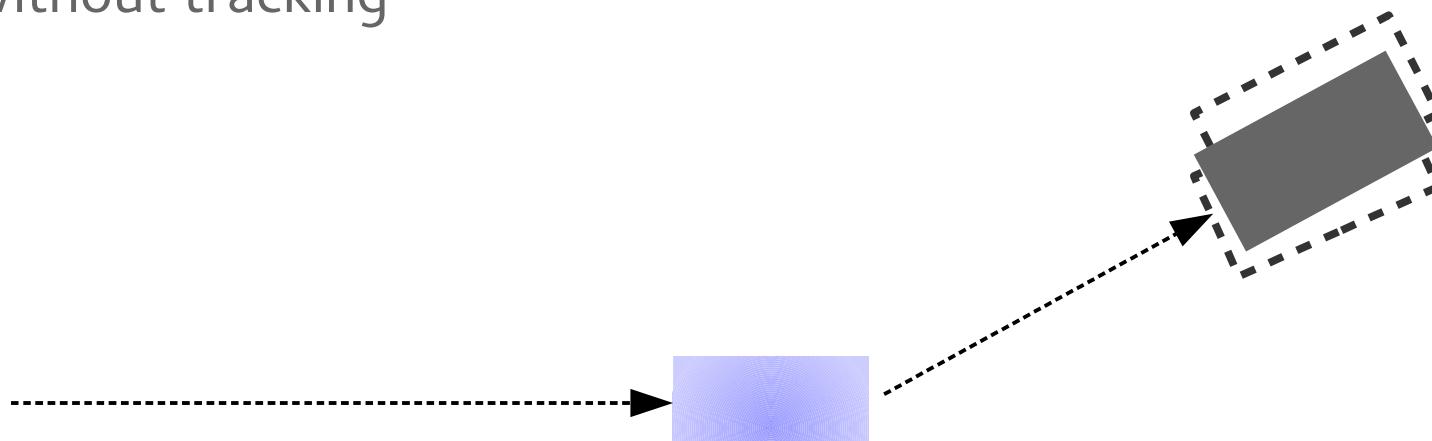


$$A_{PV} = \frac{N\downarrow - N\uparrow}{N\downarrow + N\uparrow} = \frac{\sigma\downarrow - \sigma\uparrow}{\sigma\downarrow + \sigma\uparrow} = \frac{G_F Q^2}{4\sqrt{2}\pi\alpha} (Q_W - F(Q^2))$$

# Why is tracking necessary?

Validate the acceptance, alignment, and magnetic field map

The magnetic field is anyways necessary,  
even without tracking

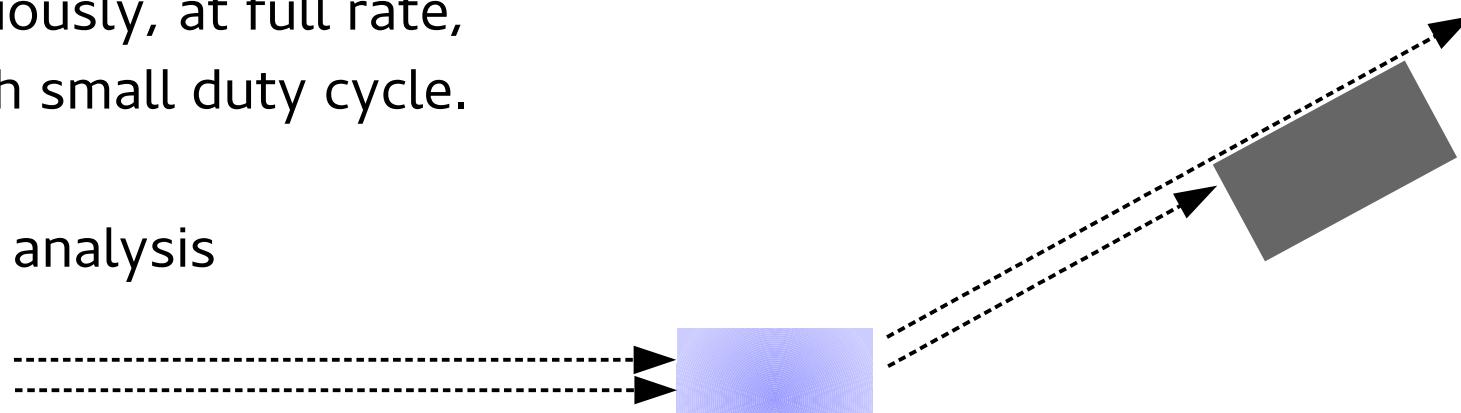


# Why is tracking necessary?

Monitor the beam and the target conditions (e.g. boiling)

Continuously, at full rate,  
but with small duty cycle.

On-line analysis



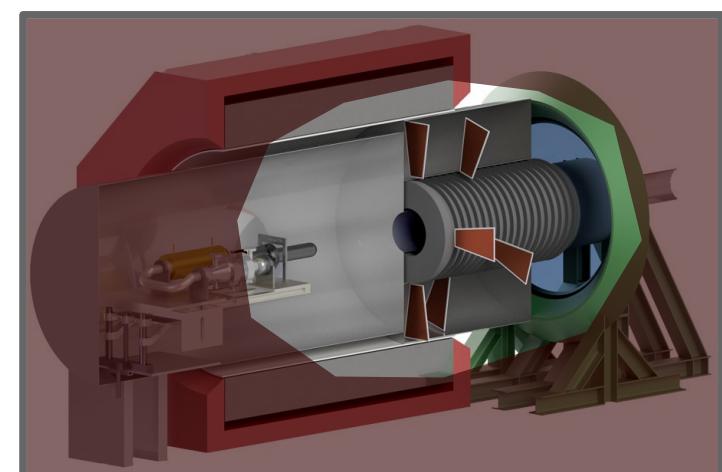
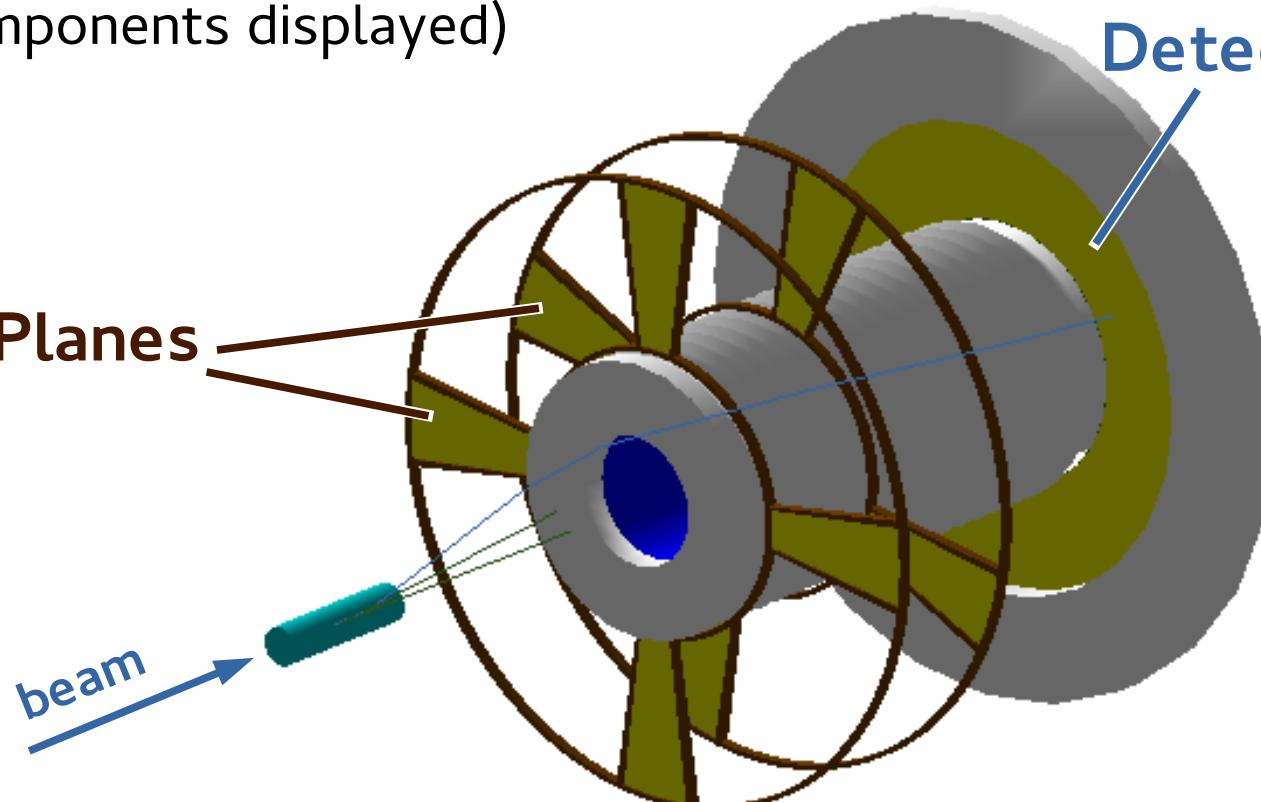
# GEANT4 simulation

(only relevant components displayed)

Tracking Planes

beam

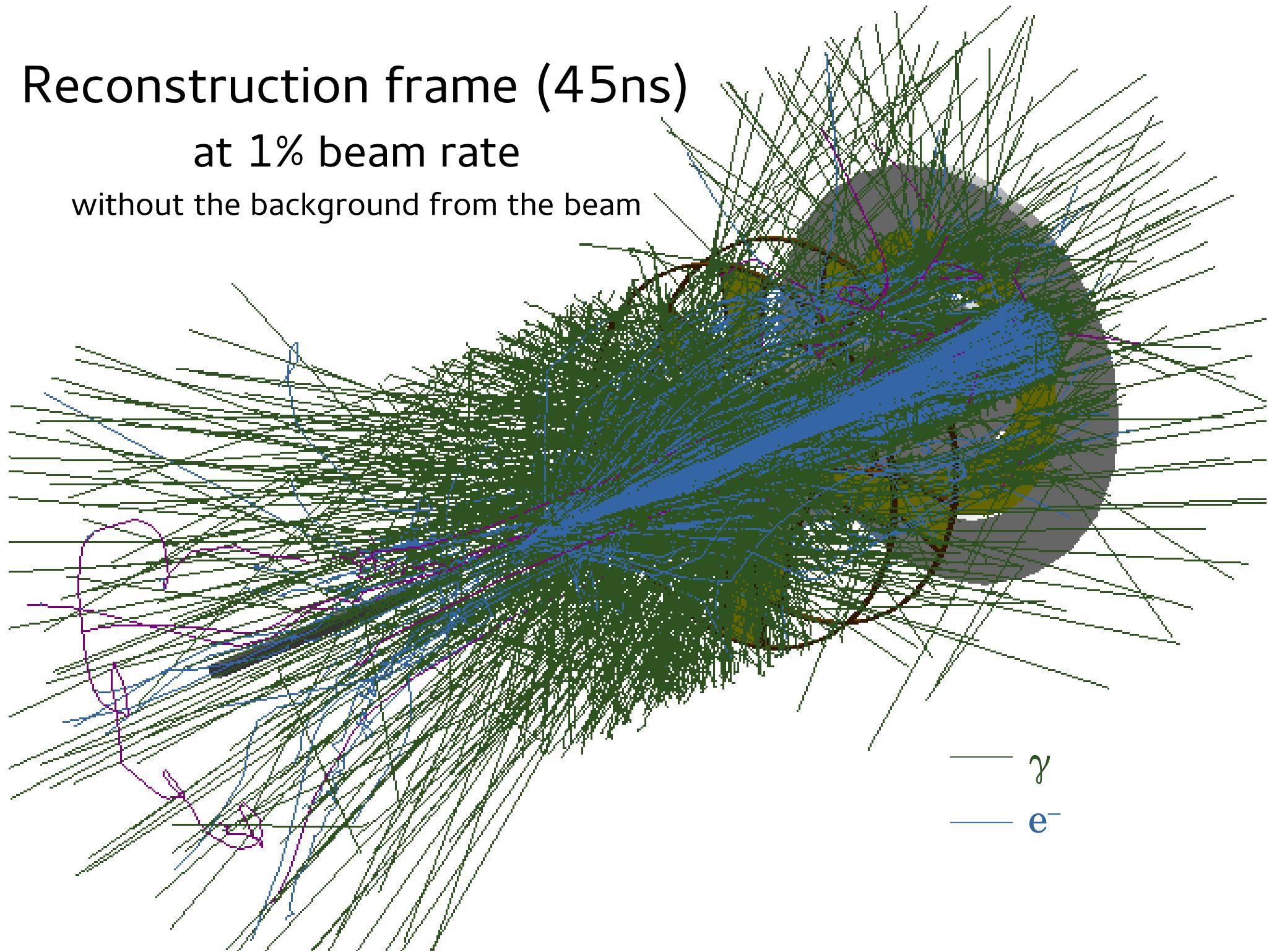
Integrating  
Cherenkov  
Detector



# Reconstruction frame (45ns)

at 1% beam rate

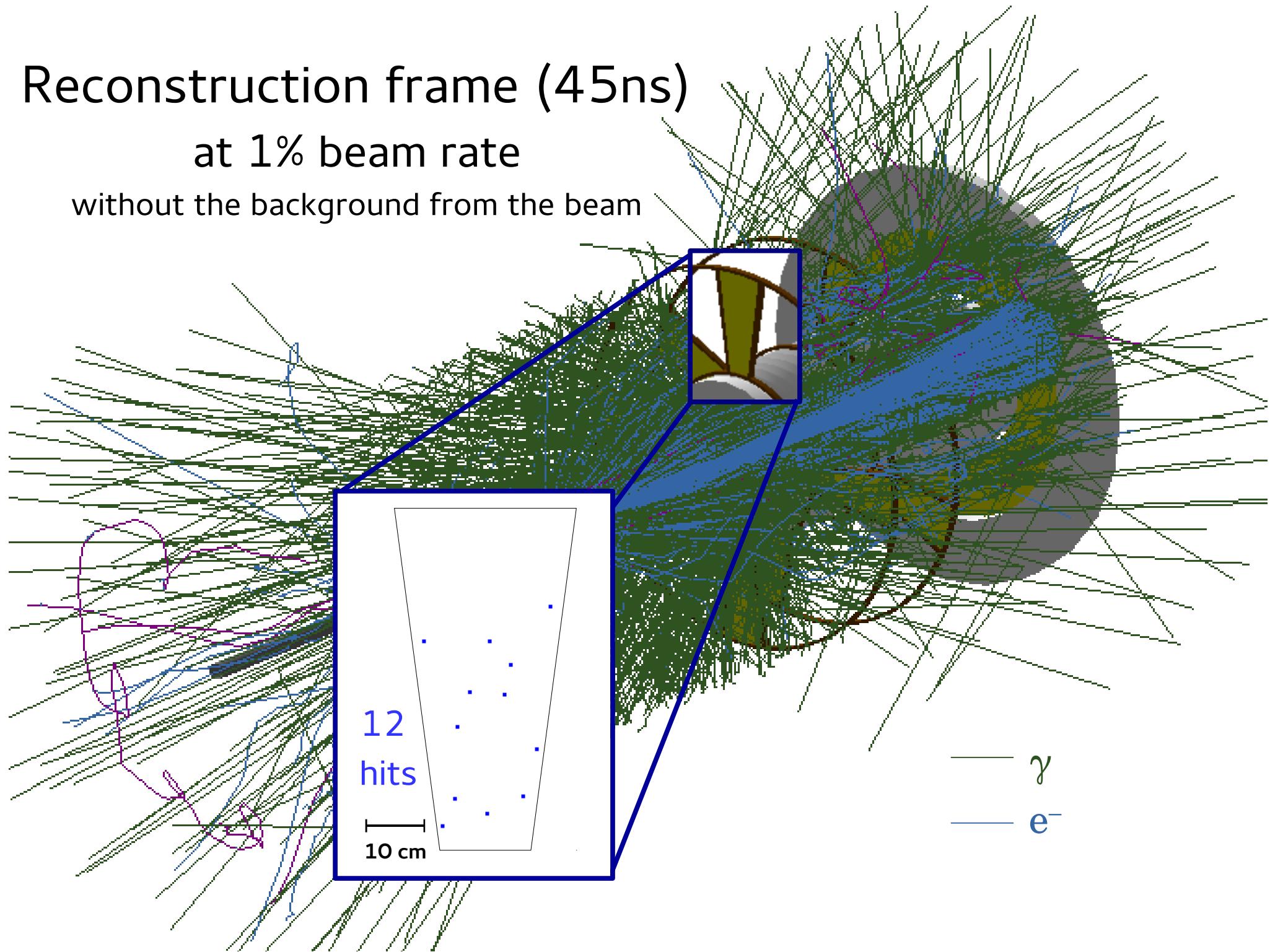
without the background from the beam



# Reconstruction frame (45ns)

at 1% beam rate

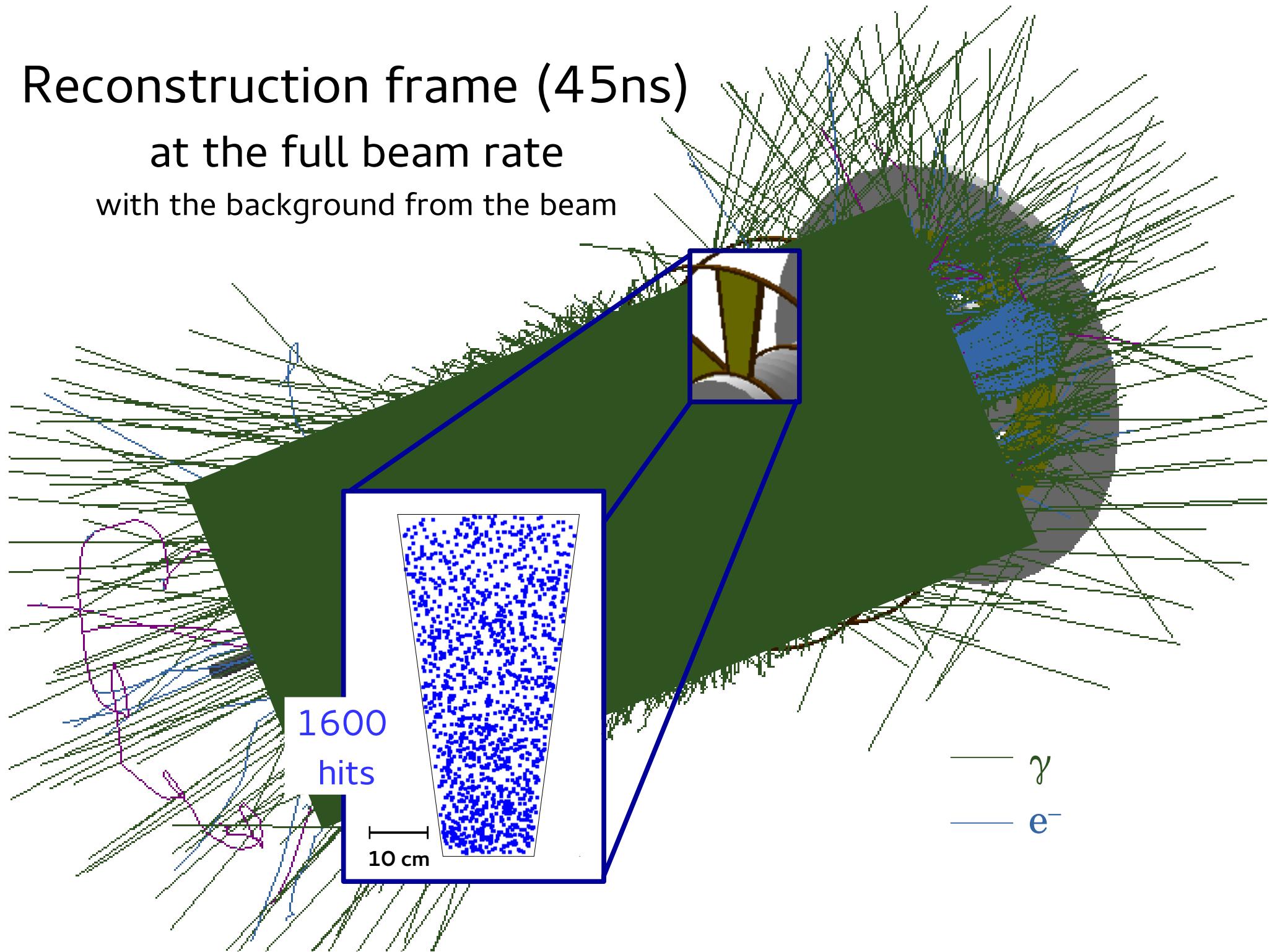
without the background from the beam



# Reconstruction frame (45ns)

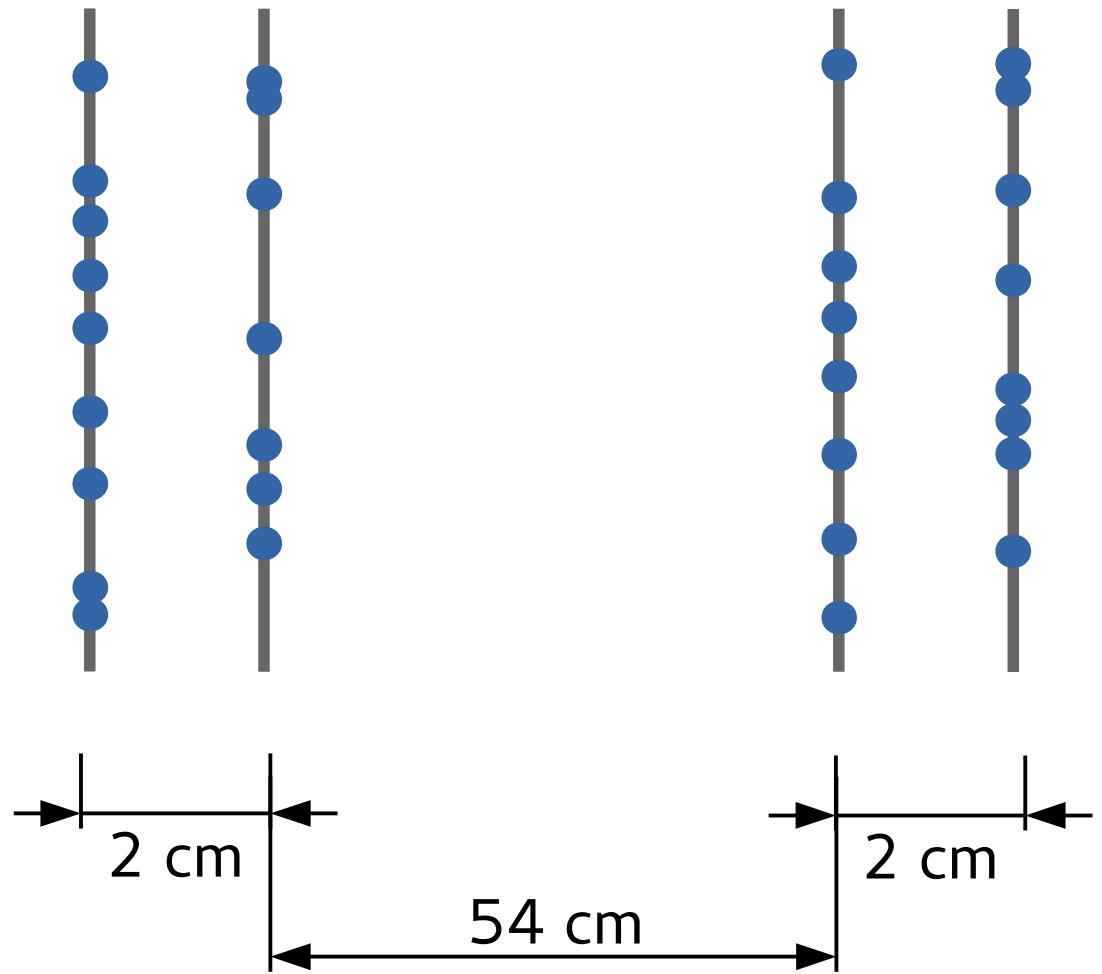
at the full beam rate

with the background from the beam

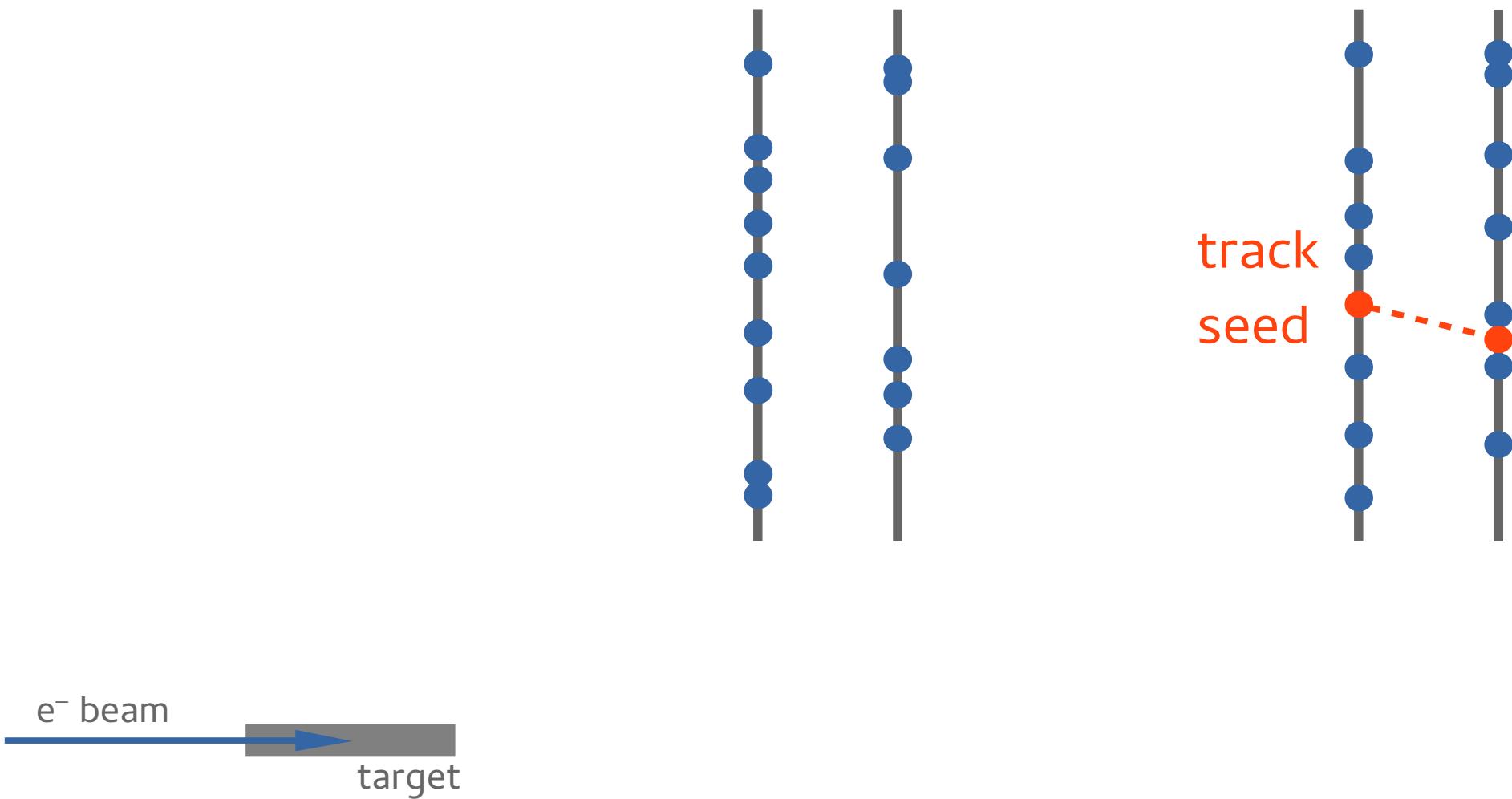


# Conventional track following

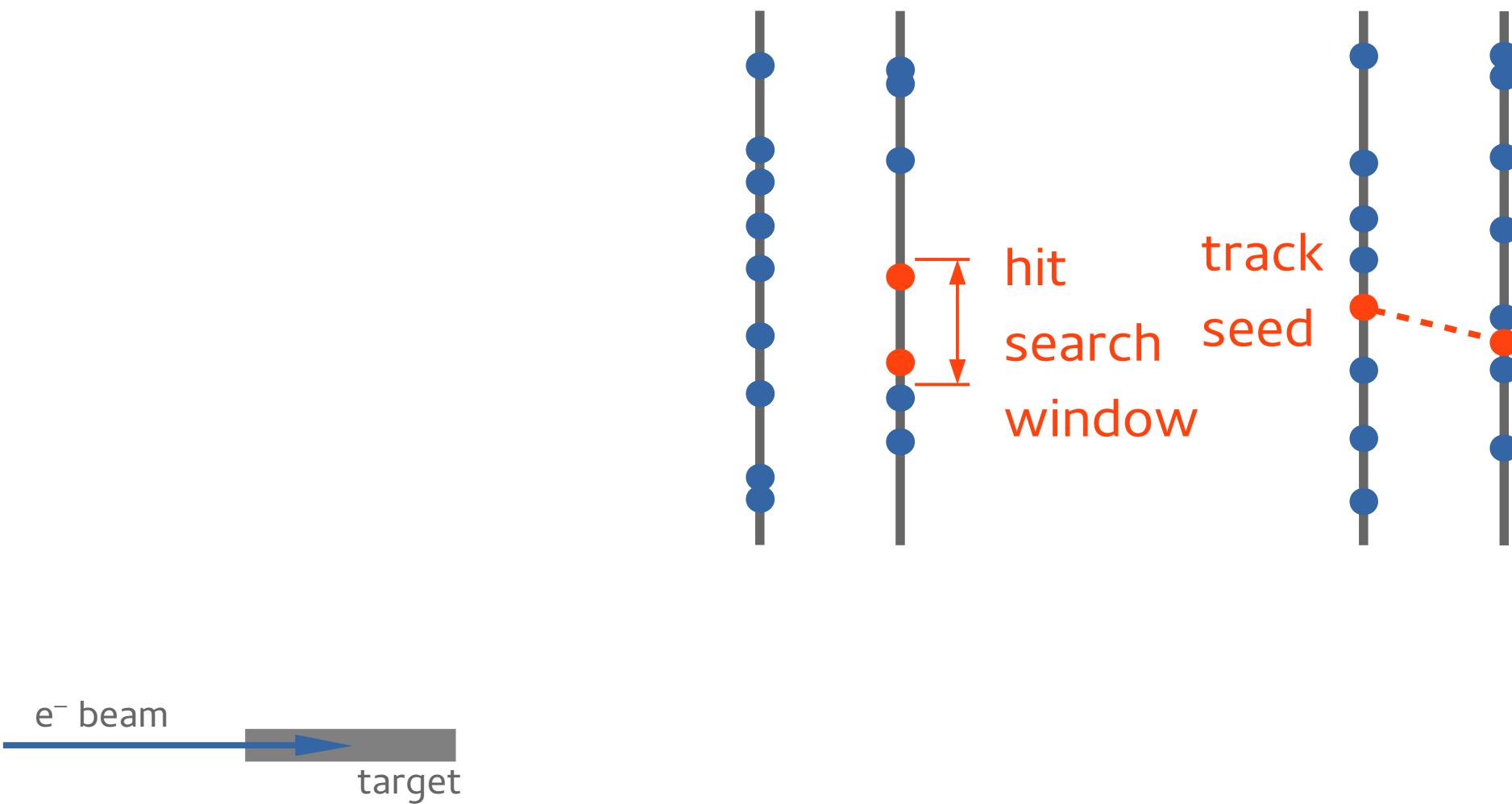
y-z view



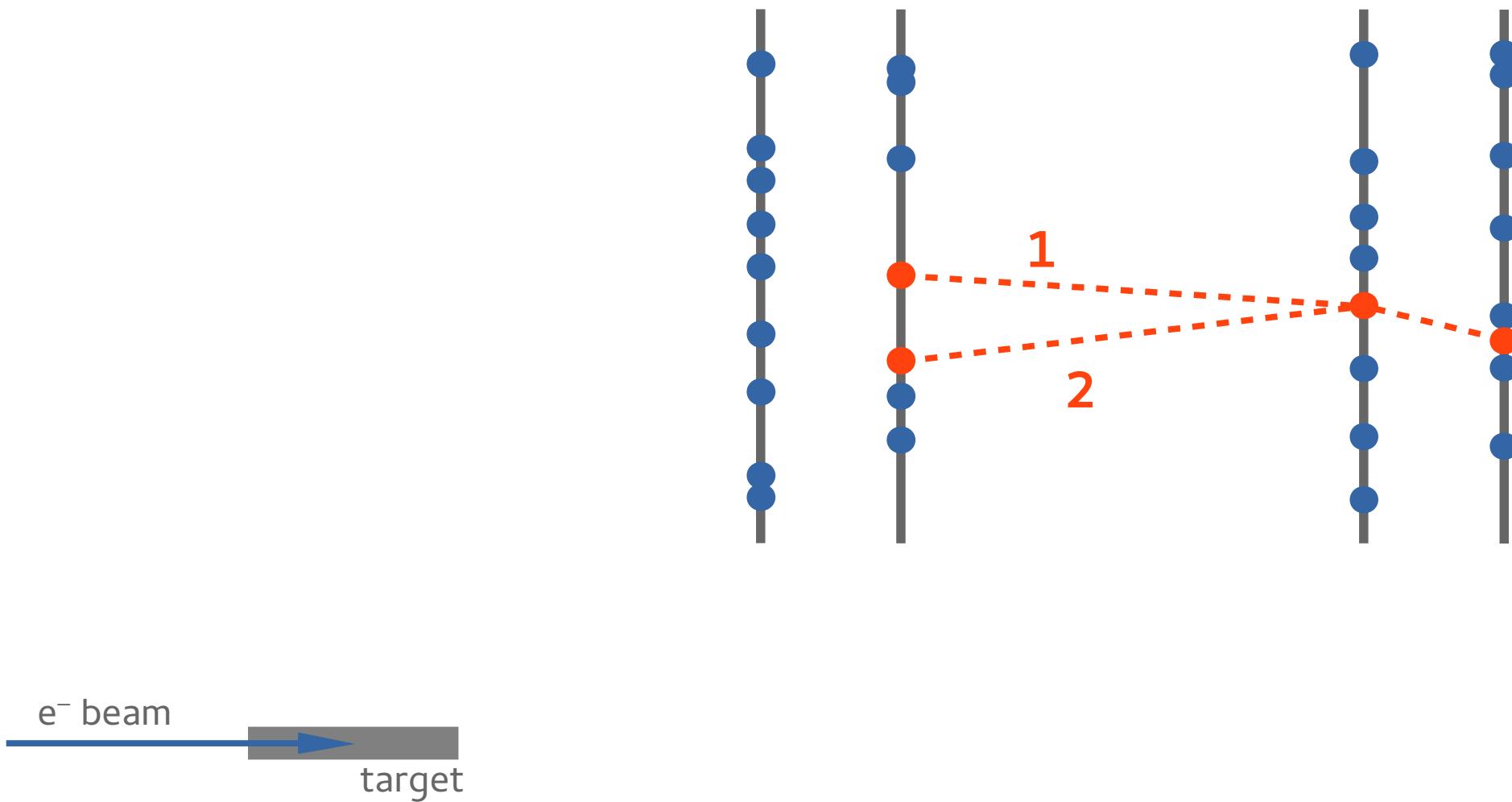
# Conventional track following



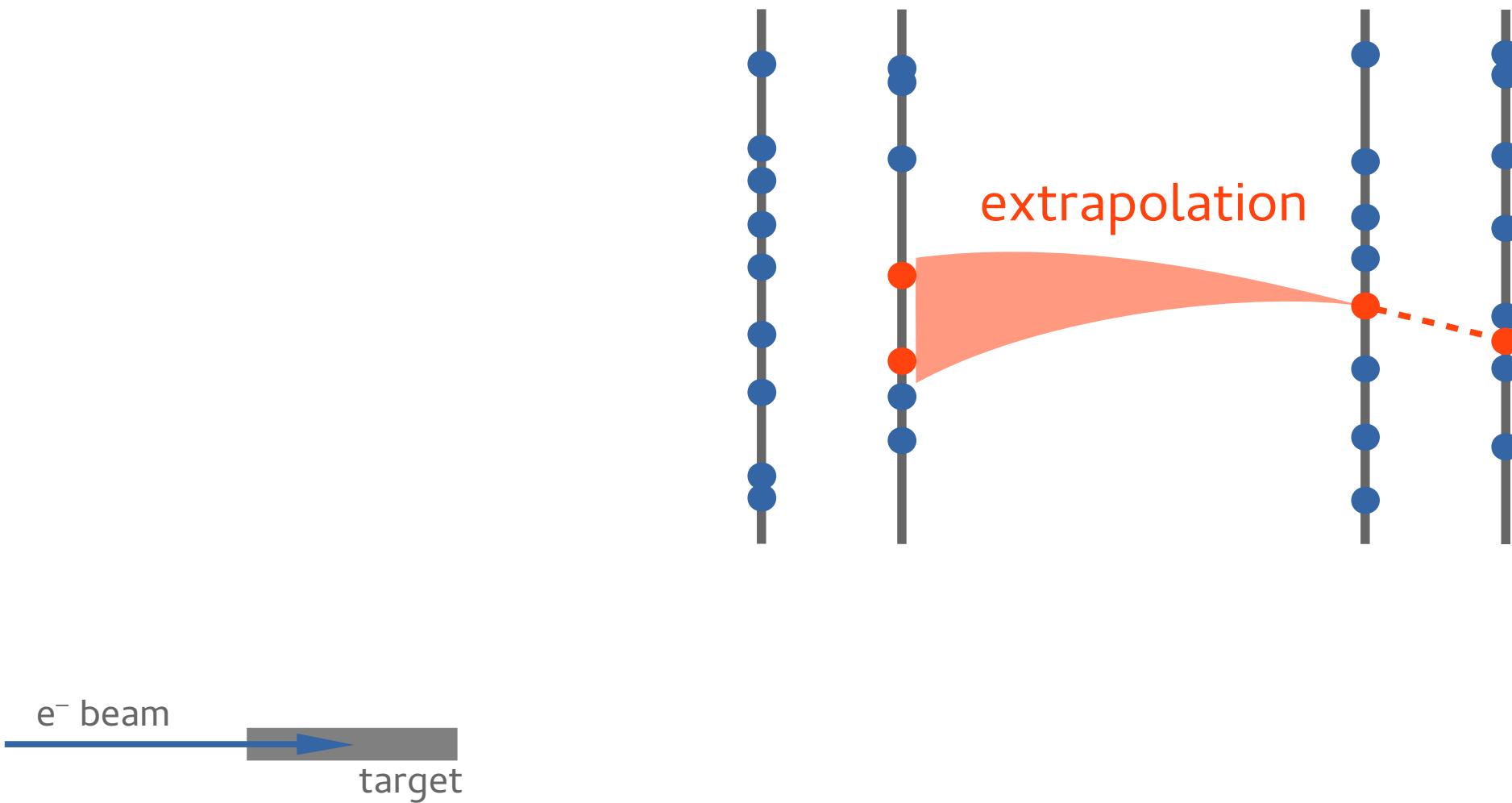
# Conventional track following



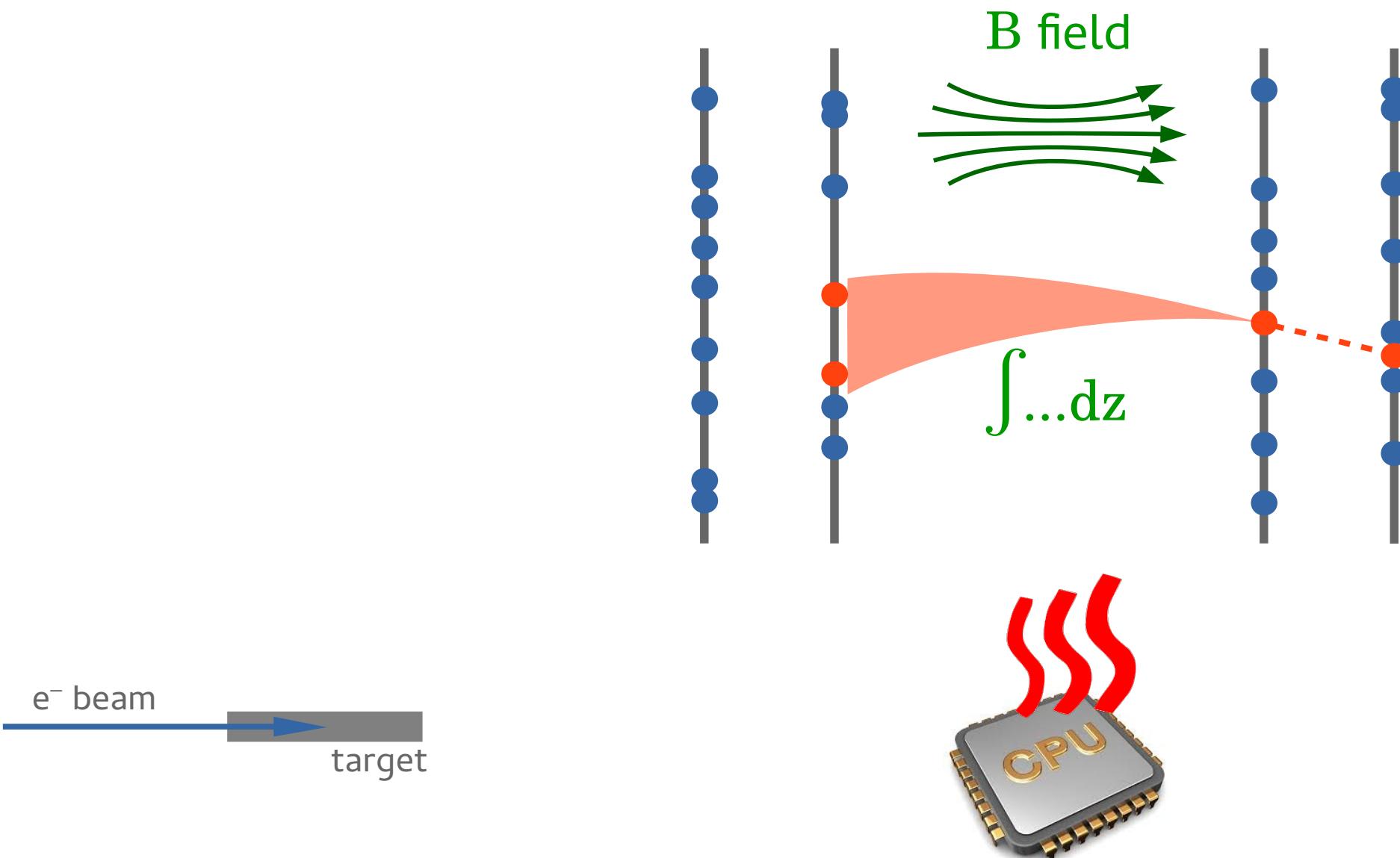
# Conventional track following



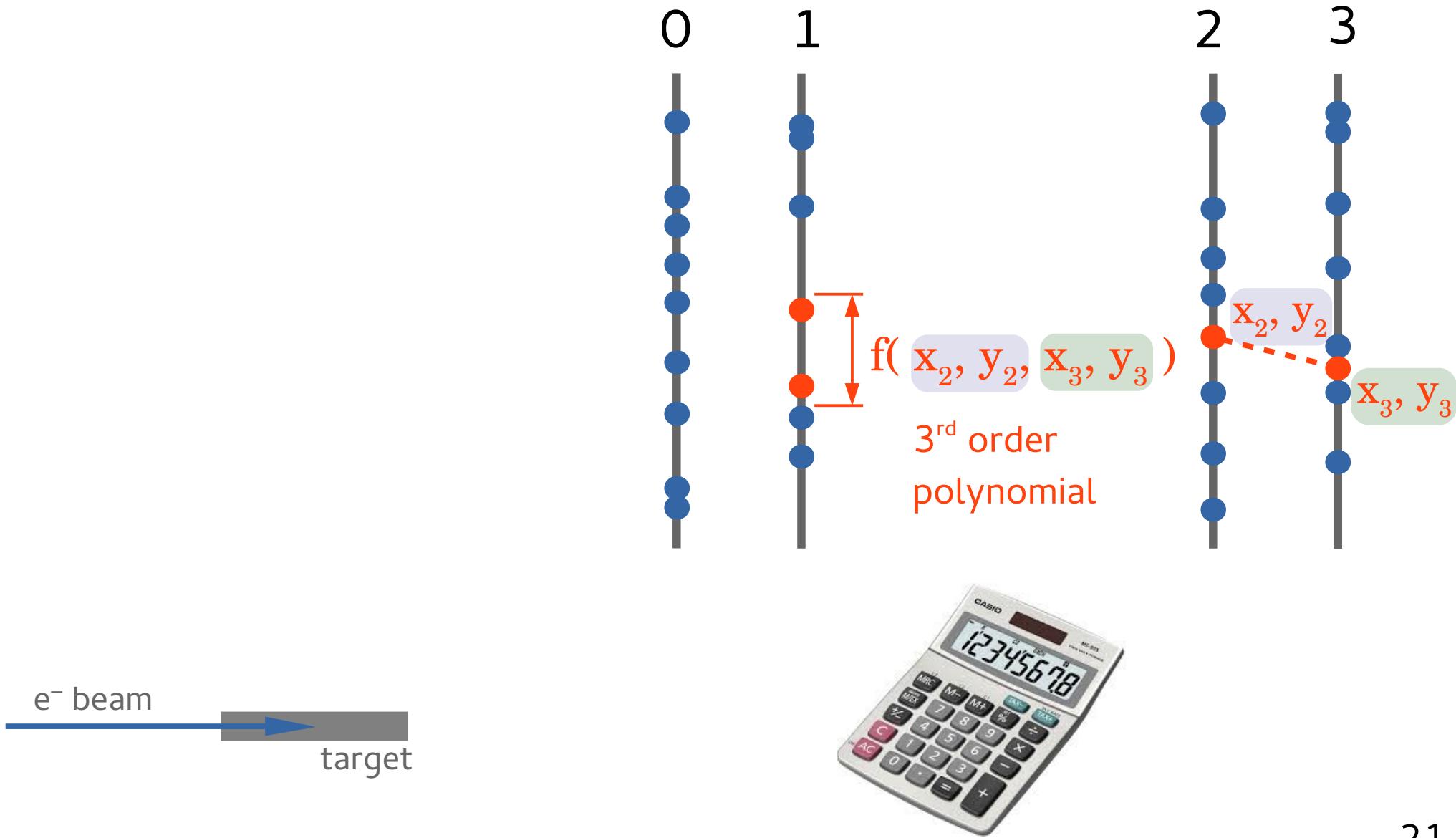
# Conventional track following



# Conventional track following

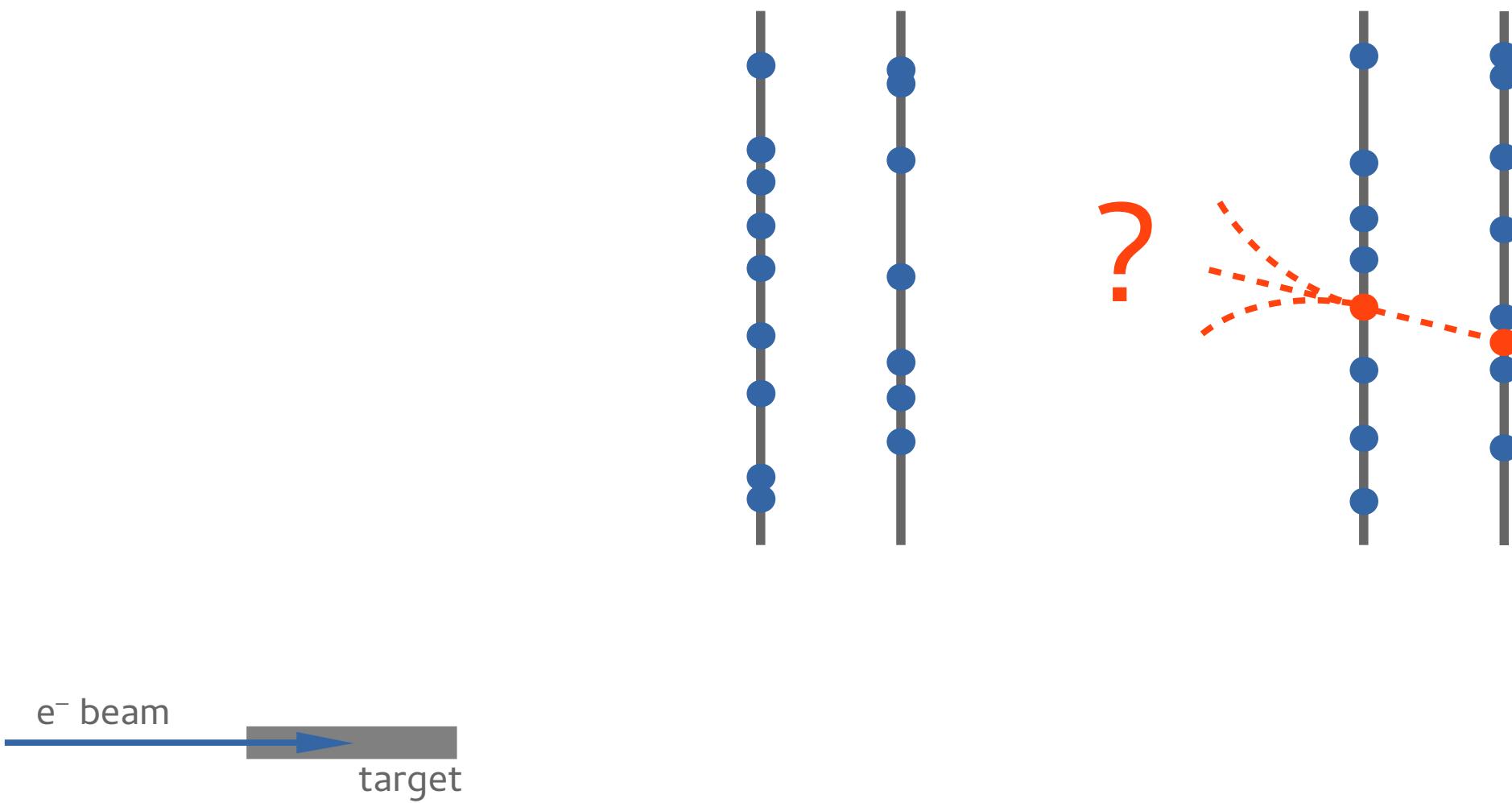


# Parameterization-based track finding

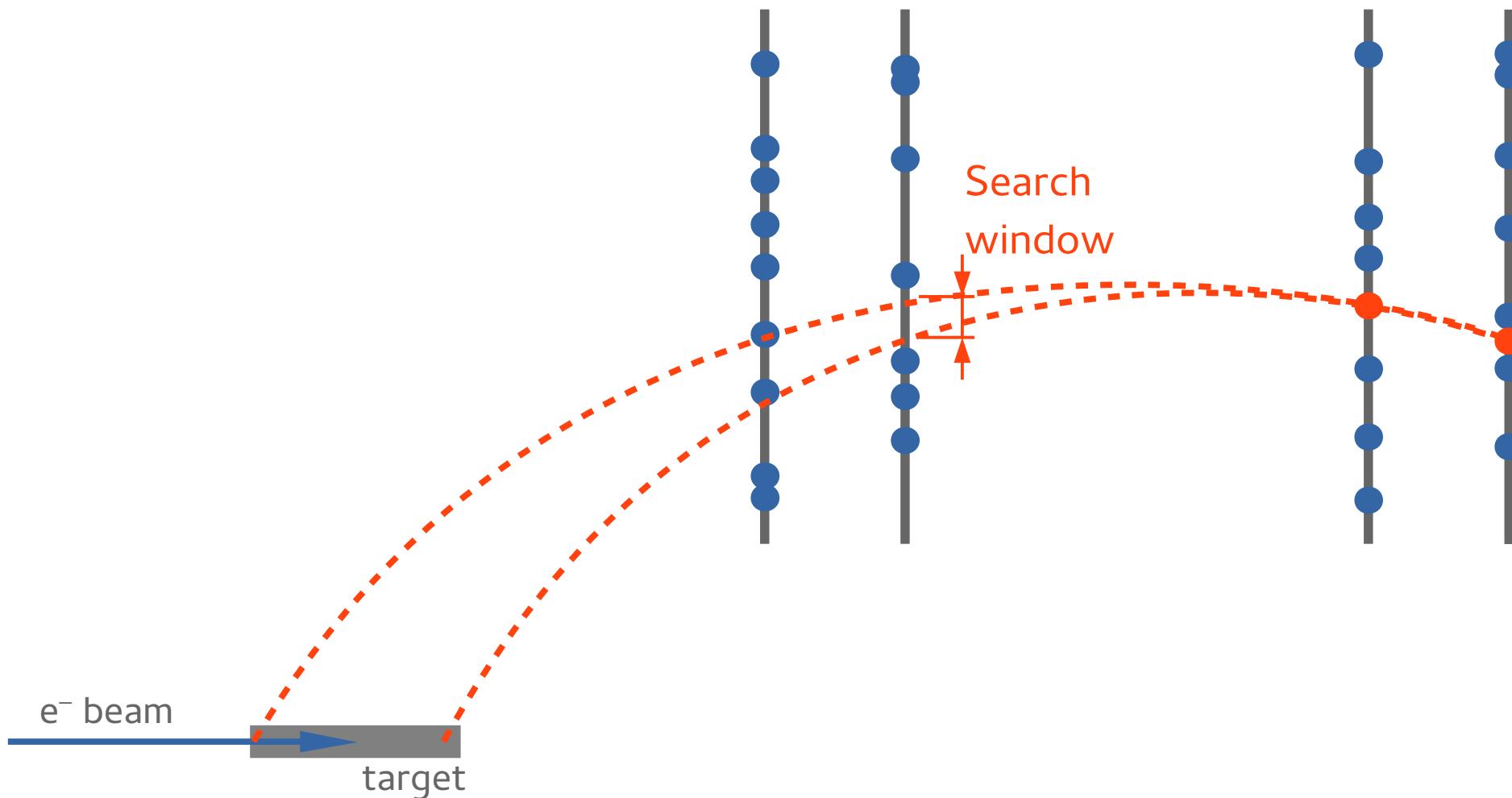


# Extrapolation

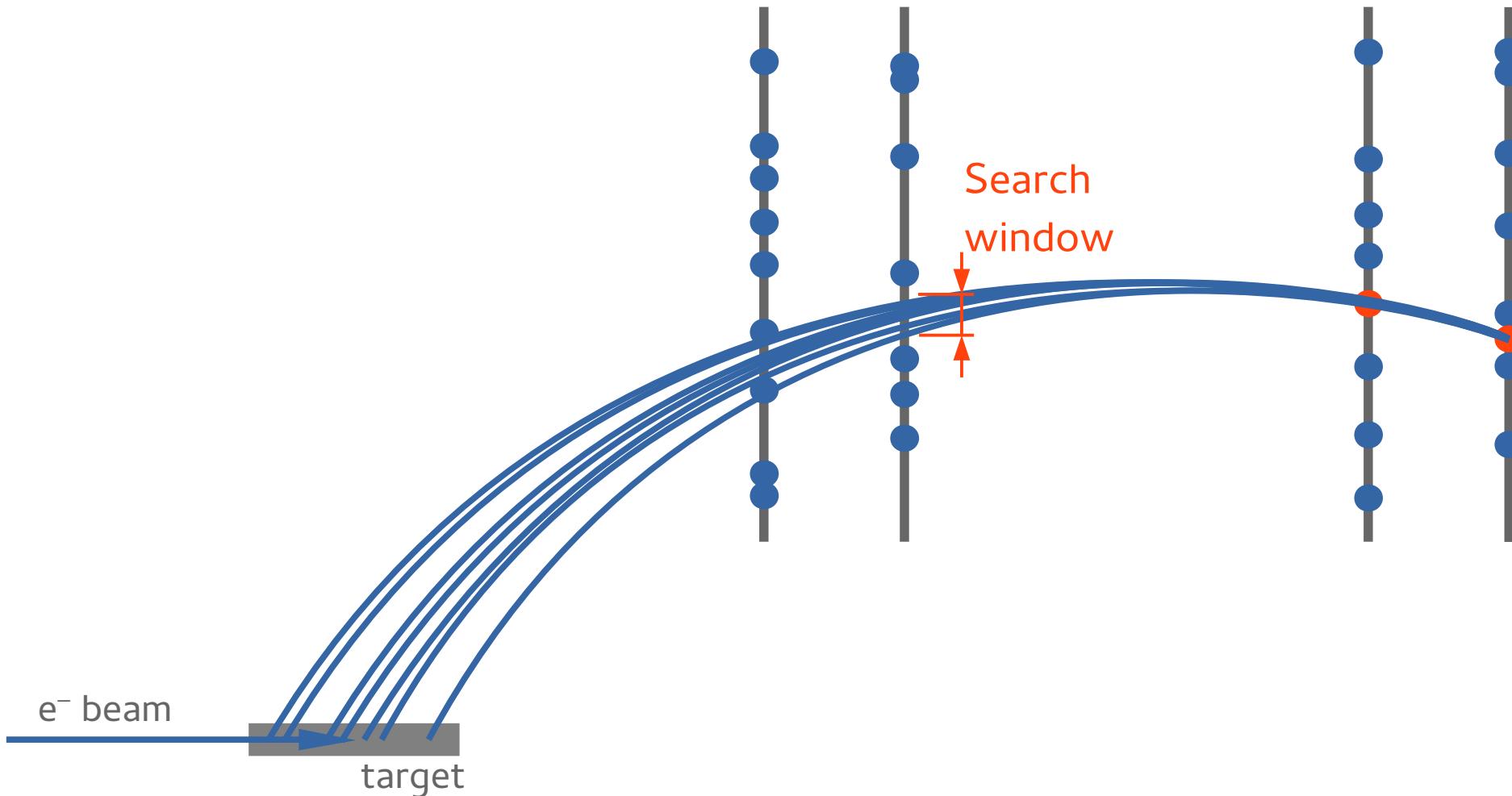
# Extrapolation



# Extrapolation with constraints

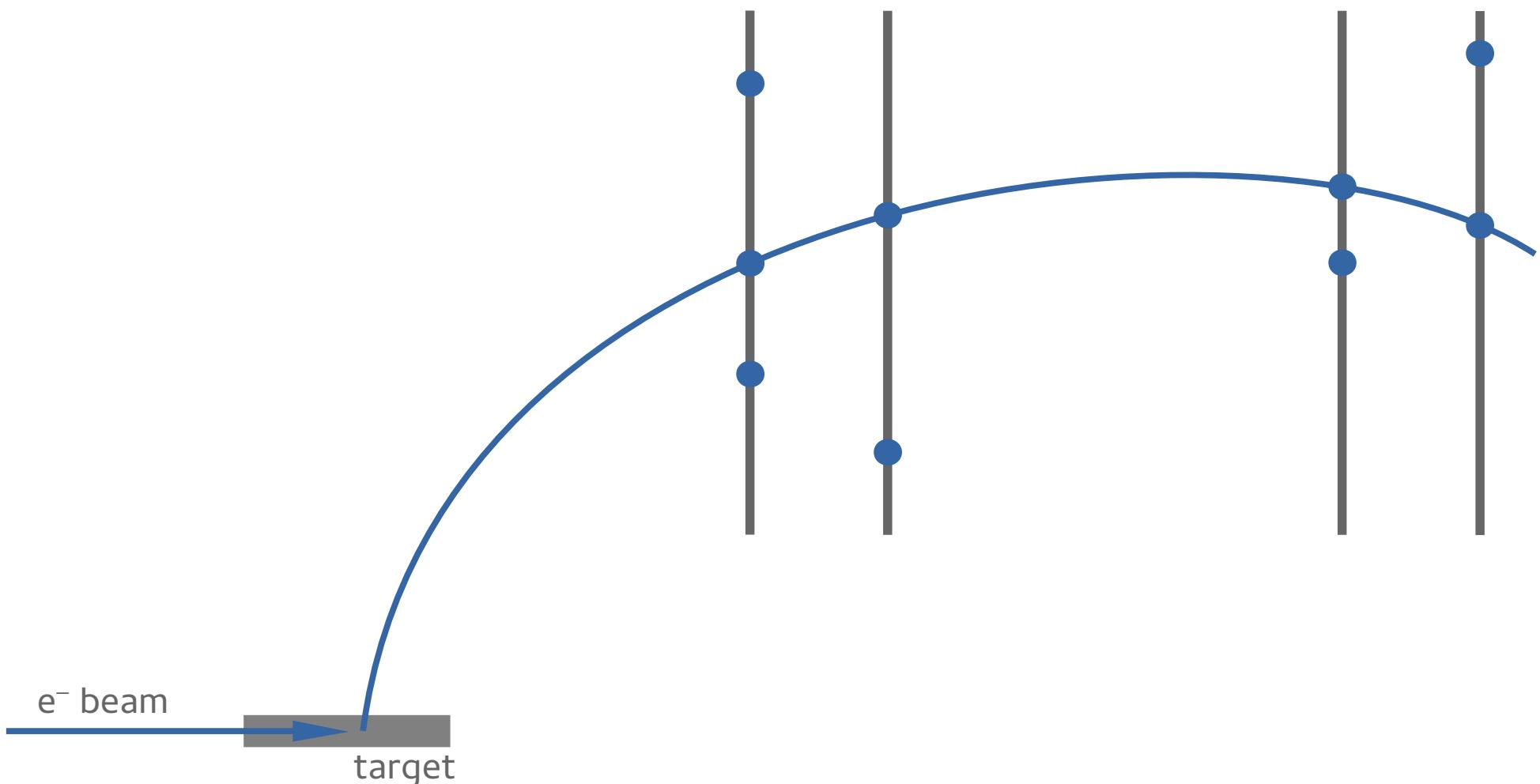


# Using reference tracks instead of extrapolation



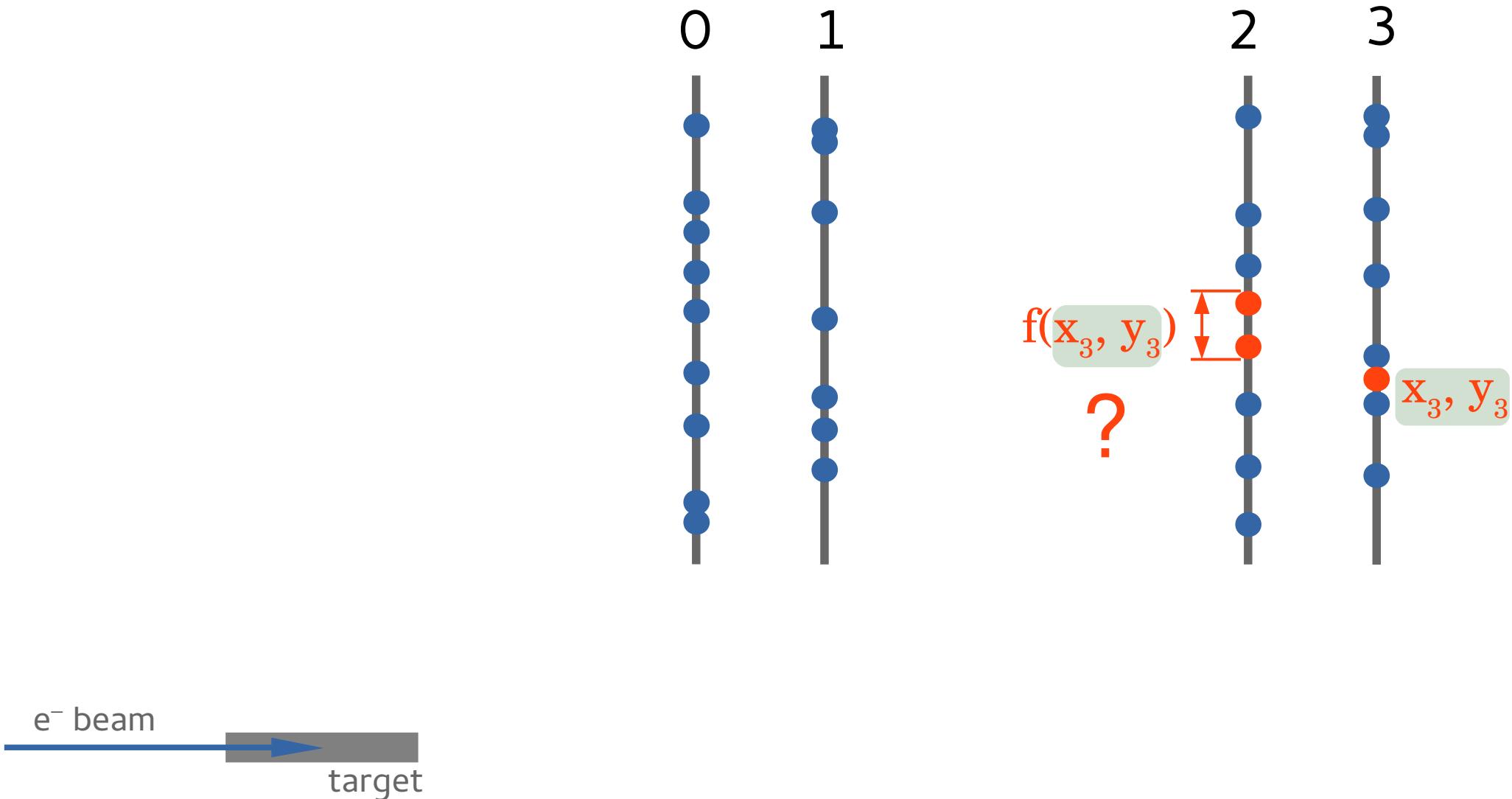
# Reference tracks:

- ▶ from MC
- ▶ brute-force reconstruction at low rate; select by  $\chi^2$ .

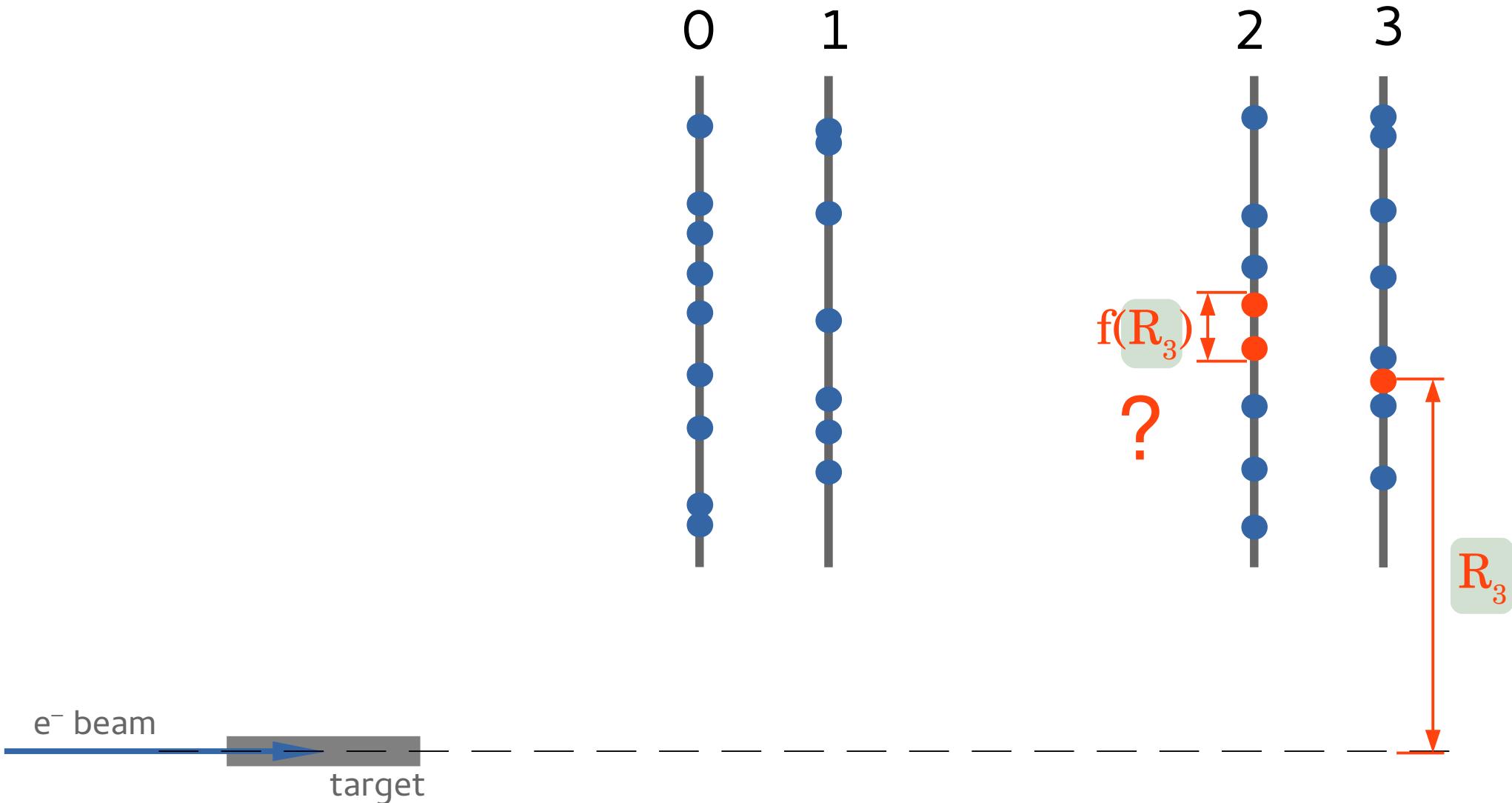


How to construct the parameterizations?

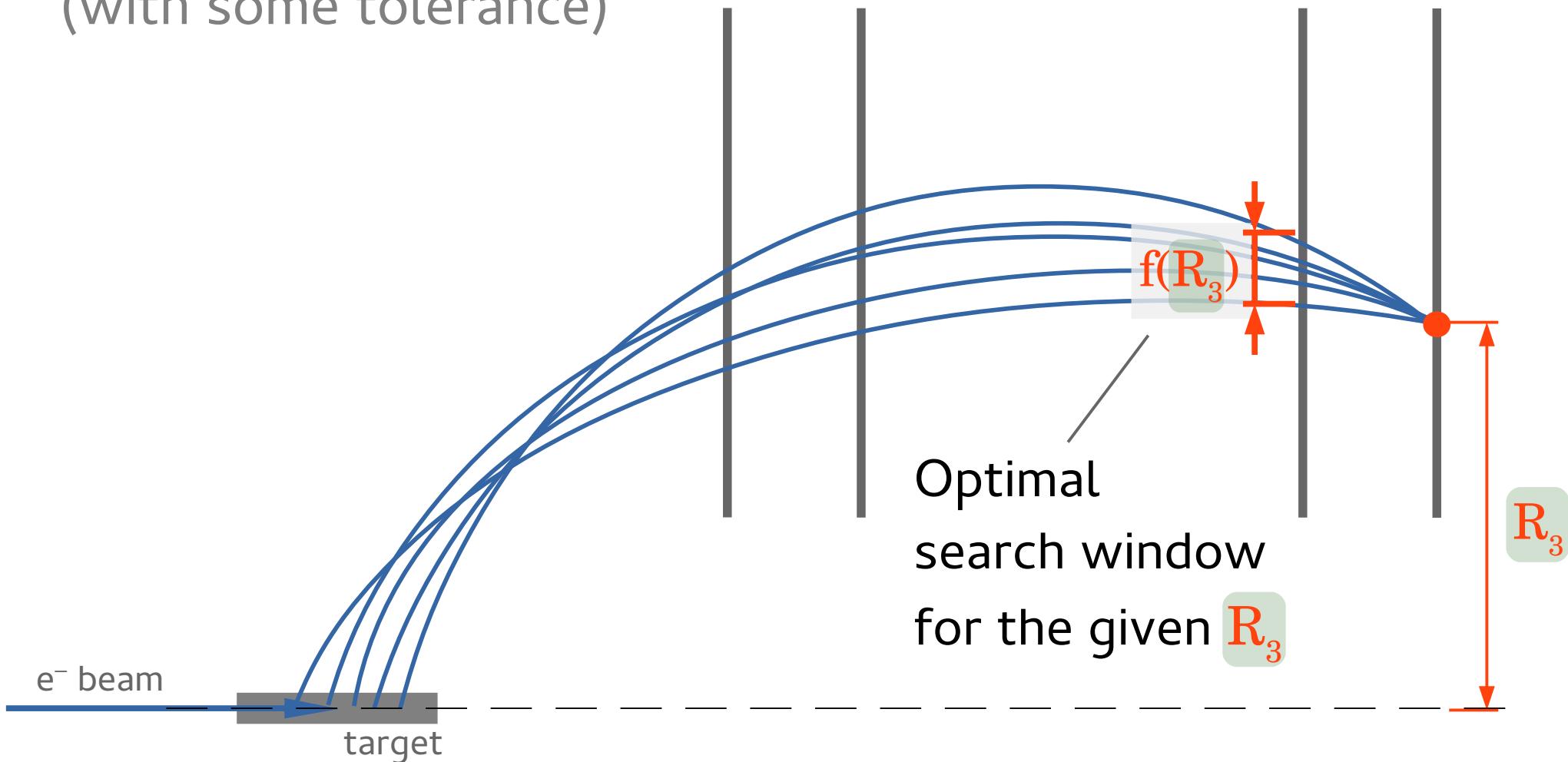
# Search window for plane 2



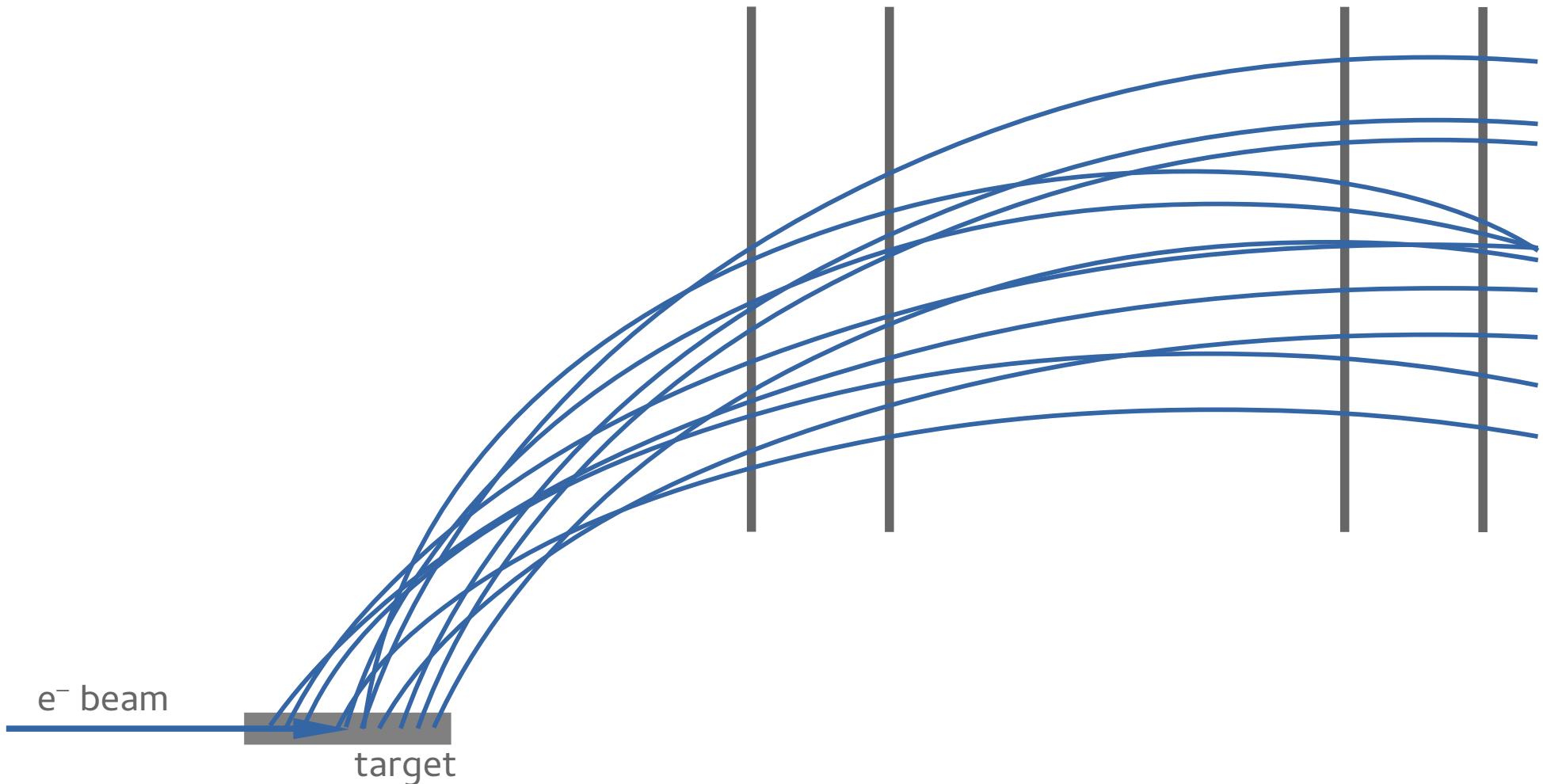
# Search window for plane 2



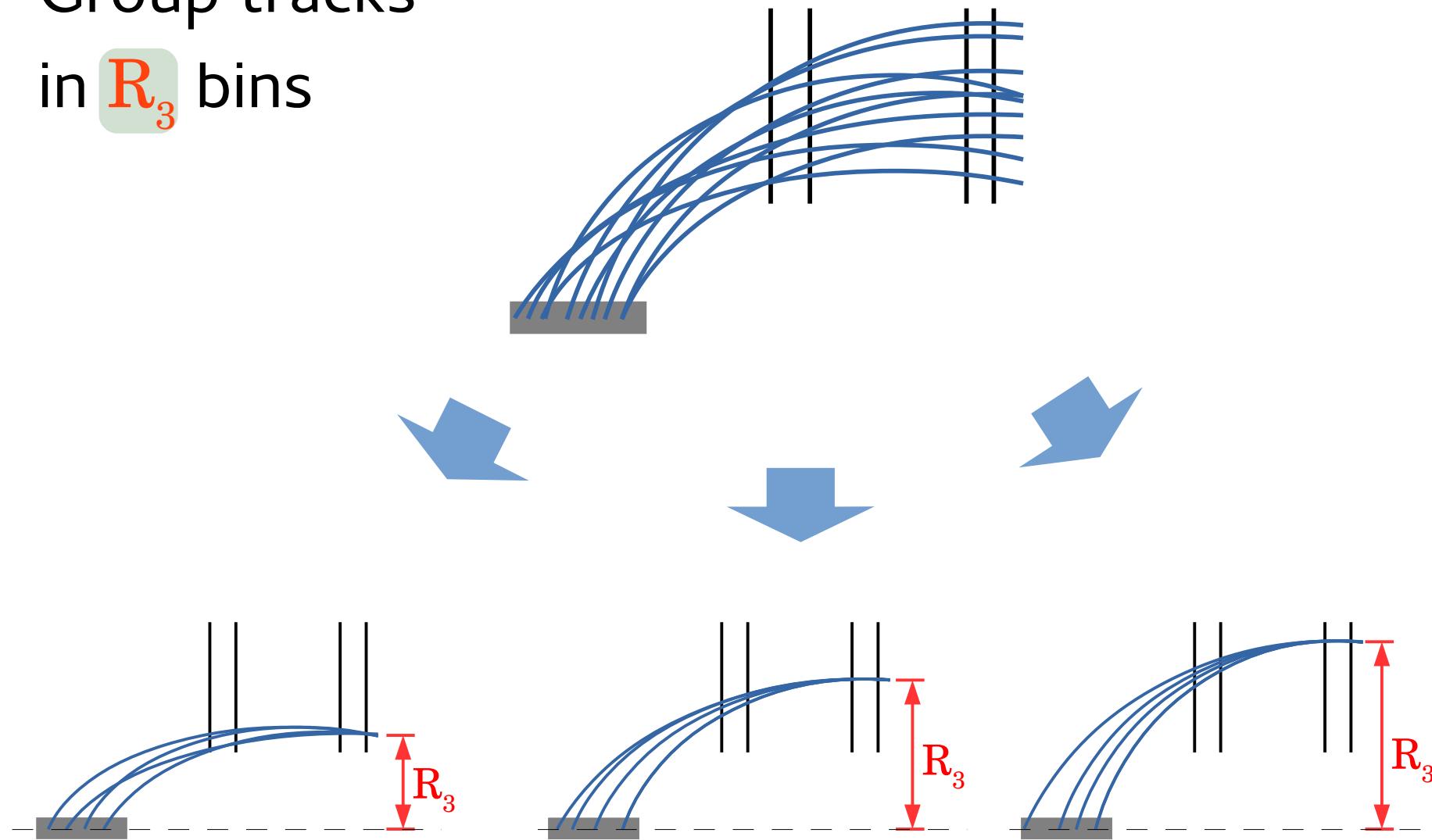
Take reference tracks  
with the given  $R_3$   
(with some tolerance)

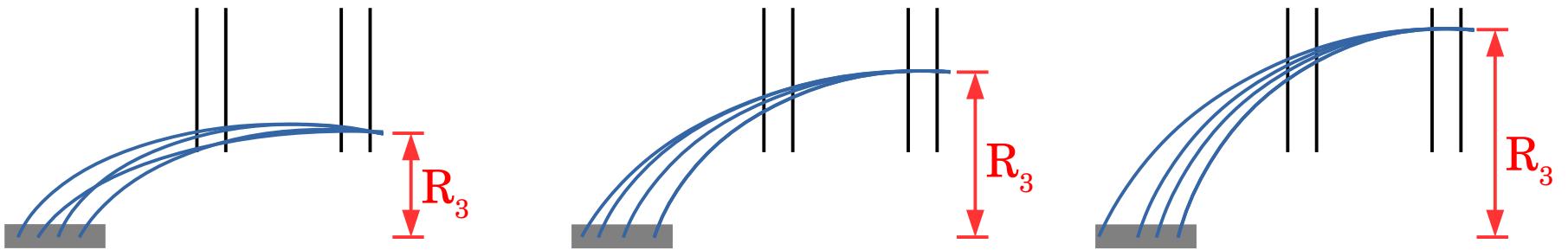


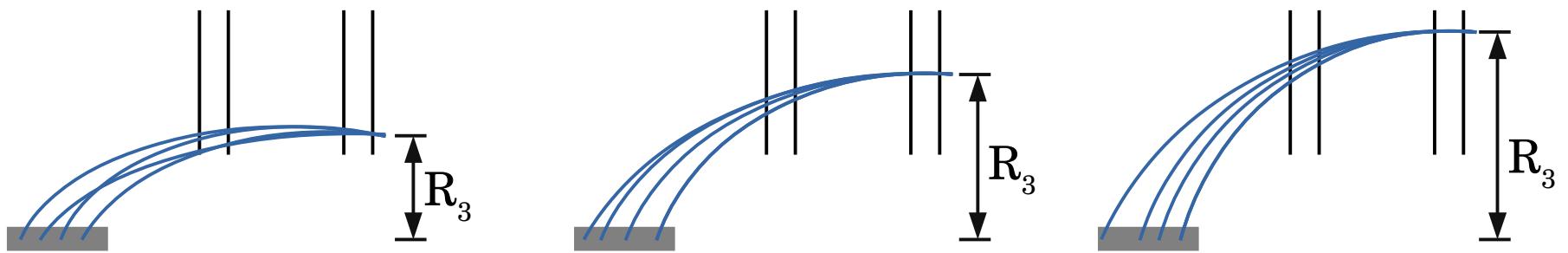
Take large number of  
reference tracks



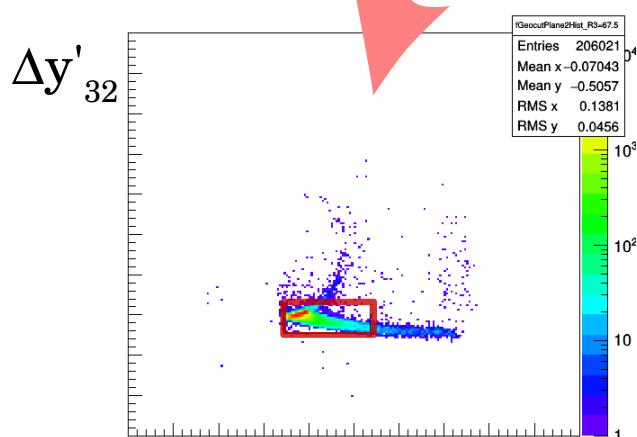
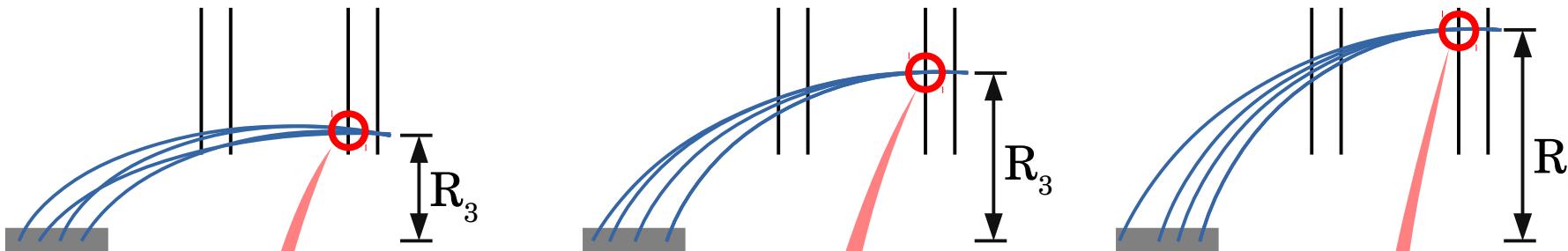
# Group tracks in $R_3$ bins



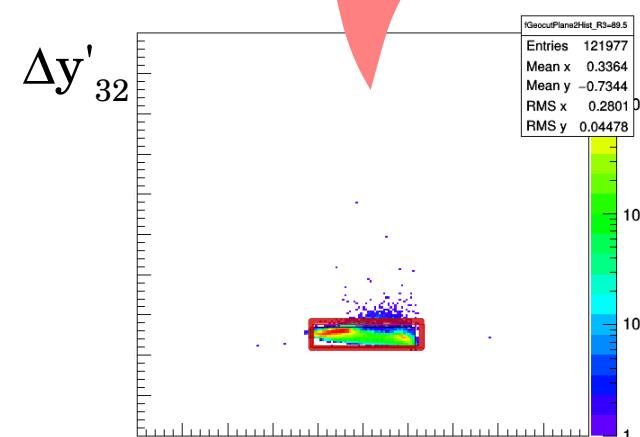




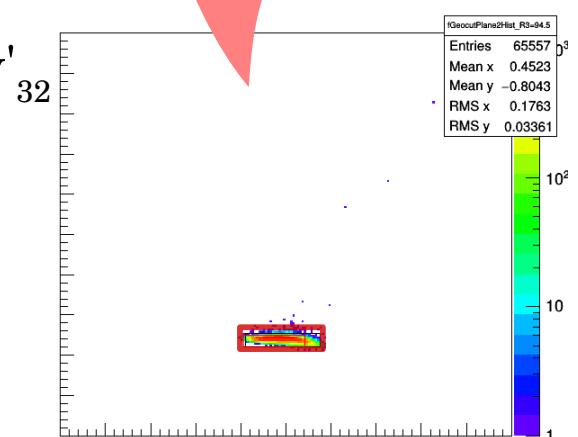
# Search window for every $R_3$ bin:



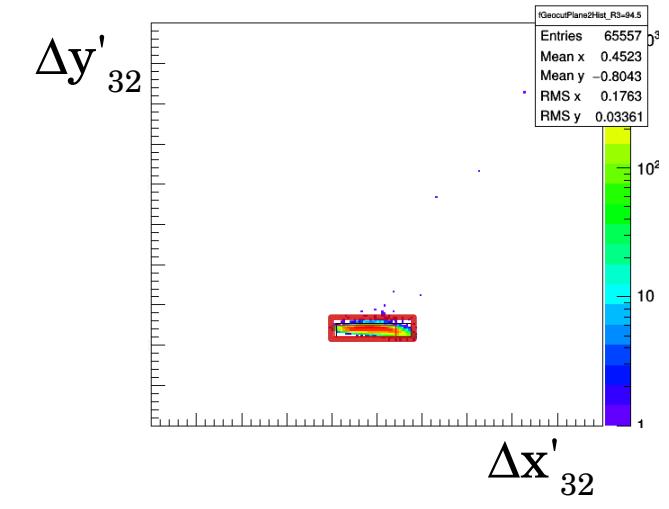
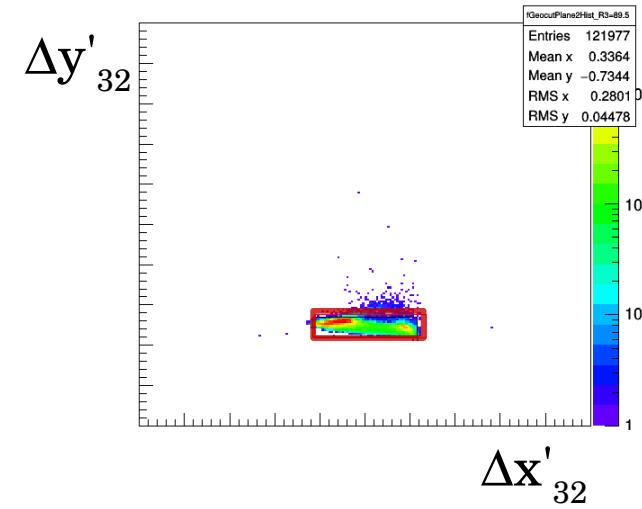
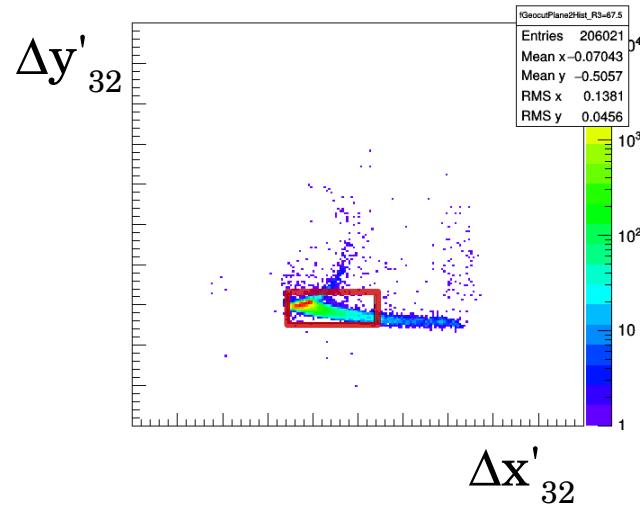
position of hit 2     $\Delta x'_{32}$   
relative to hit 3



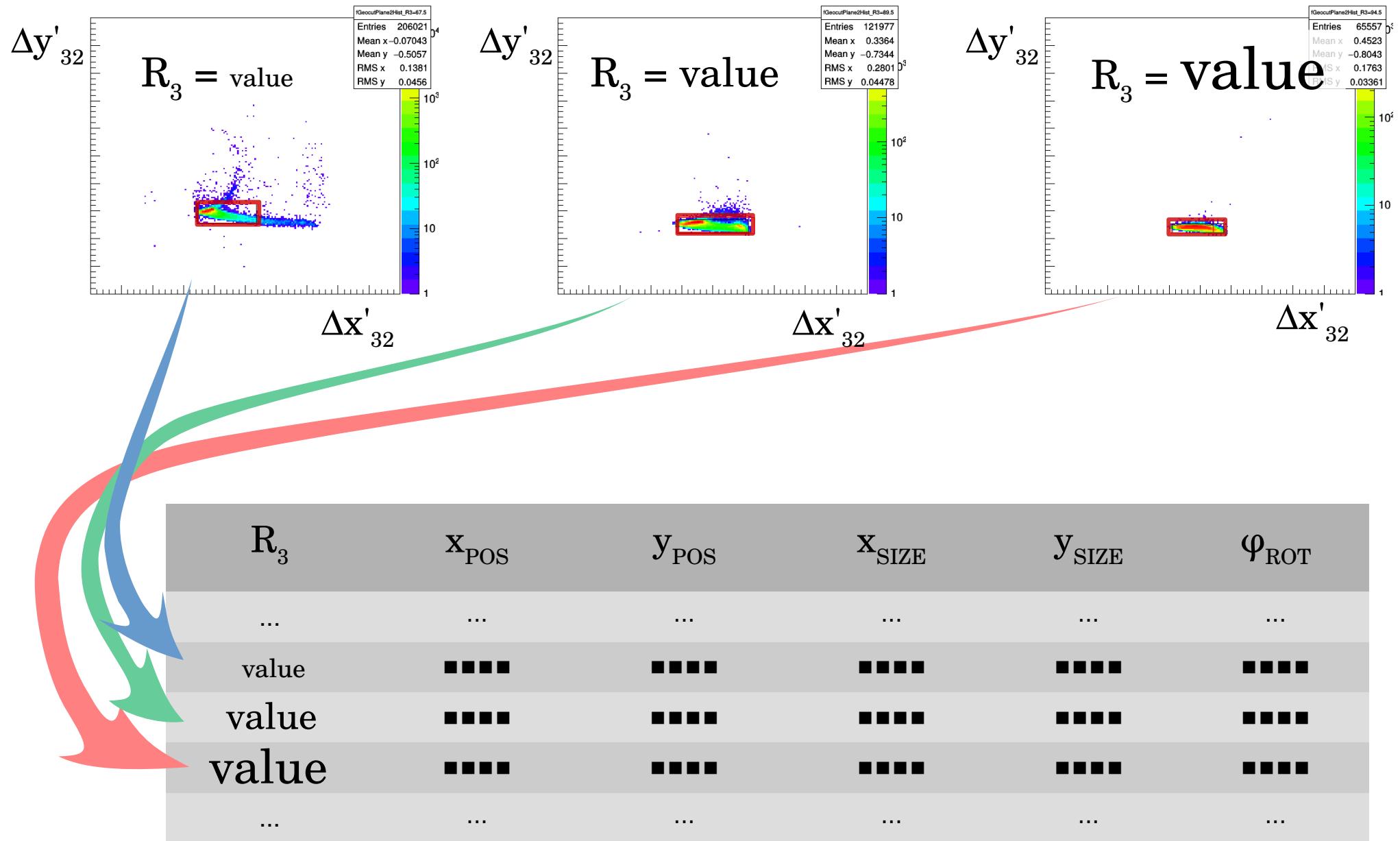
position of hit 2     $\Delta x'_{32}$   
relative to hit 3



position of hit 2     $\Delta x'_{32}$   
relative to hit 3



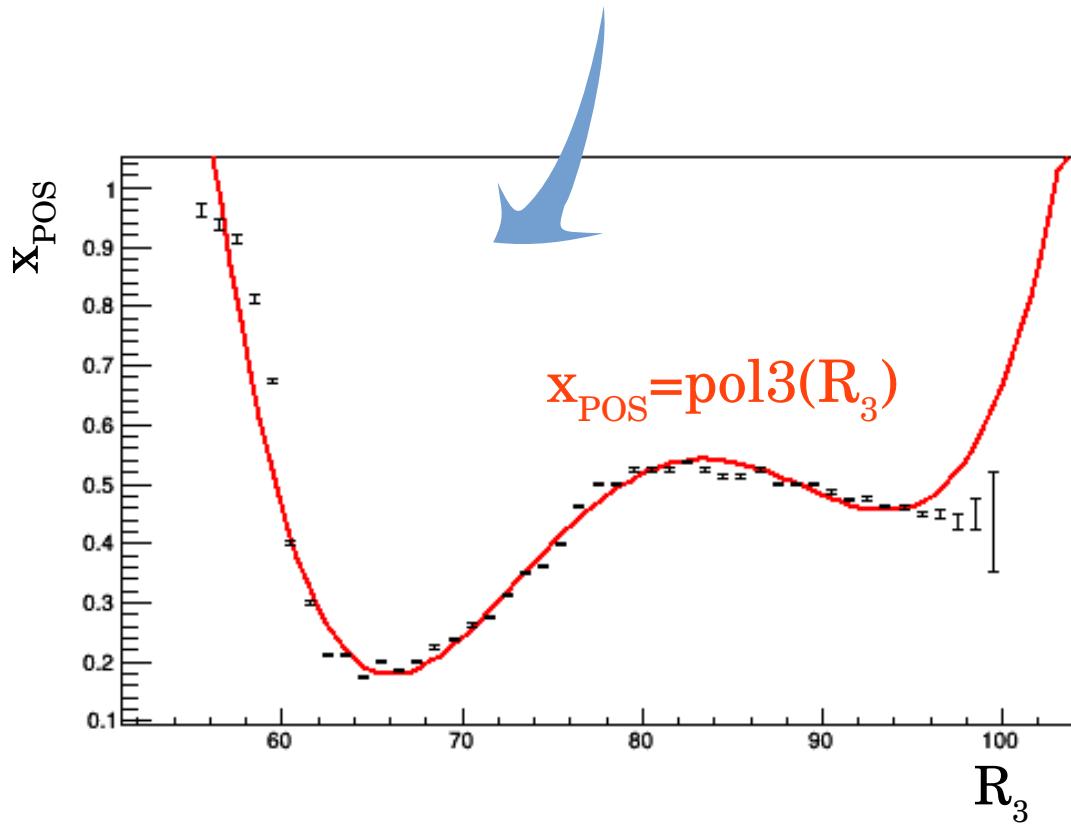
# Extract window position and size:



$R_3$	$x_{\text{POS}}$	$y_{\text{POS}}$	$x_{\text{SIZE}}$	$y_{\text{SIZE}}$	$\varphi_{\text{ROT}}$
...	...	...	...	...	...
value	■■■■	■■■■	■■■■	■■■■	■■■■
value	■■■■	■■■■	■■■■	■■■■	■■■■
value	■■■■	■■■■	■■■■	■■■■	■■■■
...	...	...	...	...	...

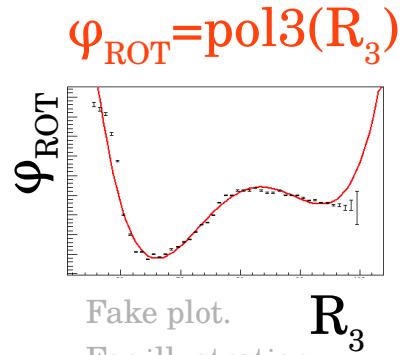
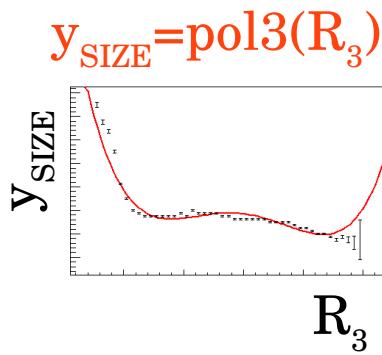
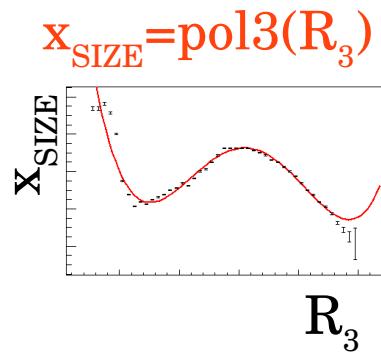
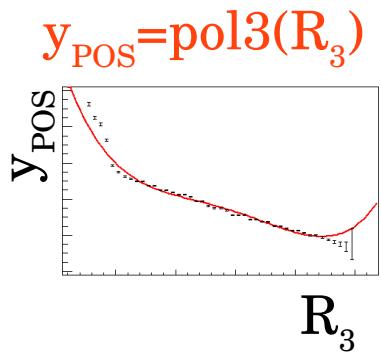
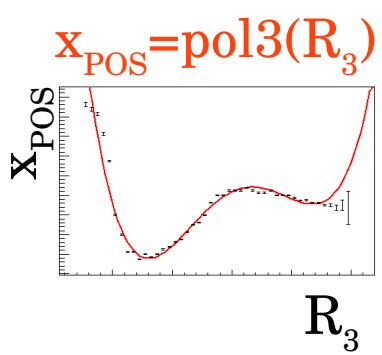
# Fit

$R_3$	$x_{\text{POS}}$	$y_{\text{POS}}$	$x_{\text{SIZE}}$	$y_{\text{SIZE}}$	$\varphi_{\text{ROT}}$
...	...	...	...	...	...
value	■■■■	■■■■	■■■■	■■■■	■■■■
value	■■■■	■■■■	■■■■	■■■■	■■■■
value	■■■■	■■■■	■■■■	■■■■	■■■■
...	...	...	...	...	...



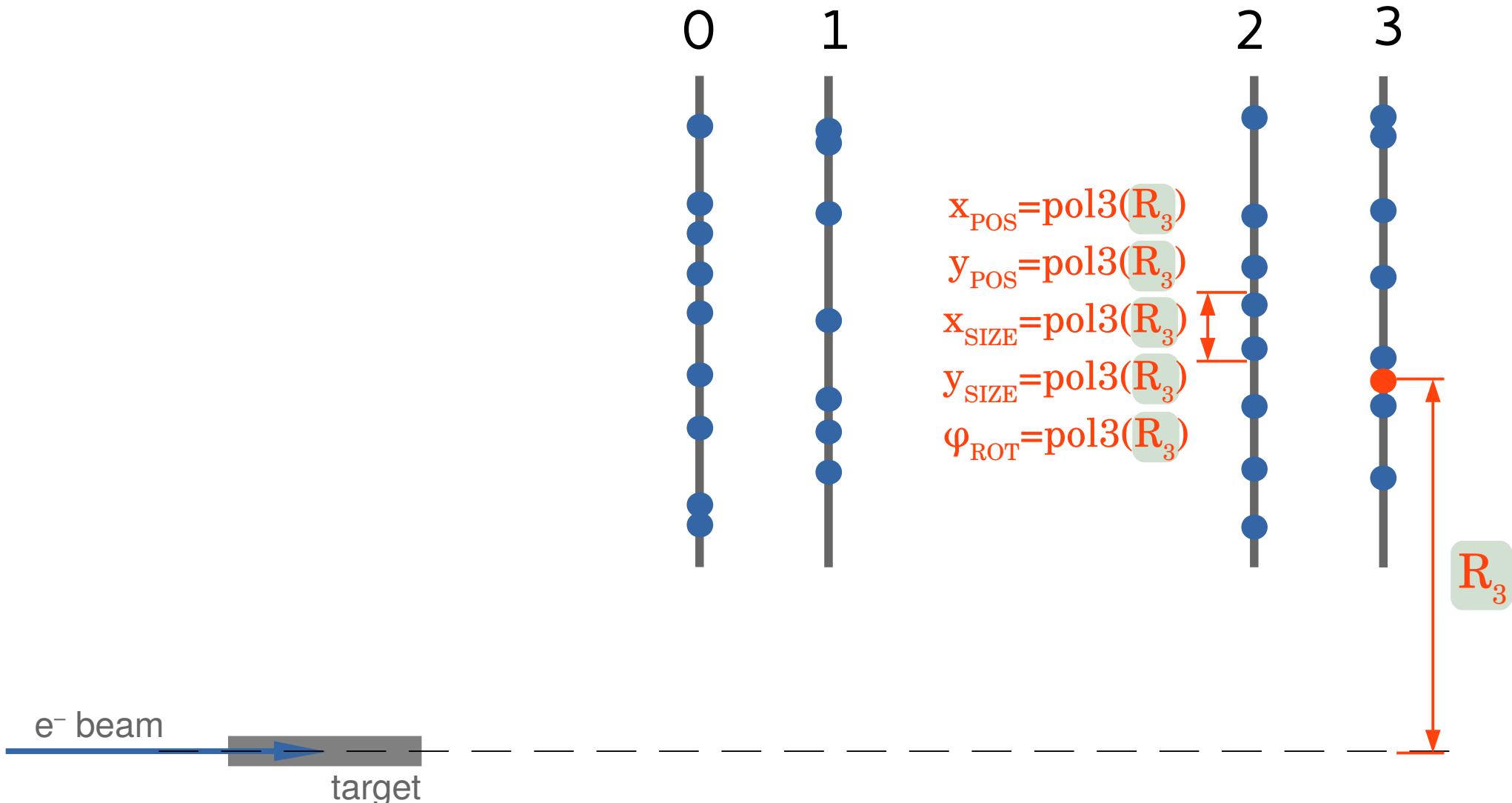
# Fit

$R_3$	$x_{\text{POS}}$	$y_{\text{POS}}$	$x_{\text{SIZE}}$	$y_{\text{SIZE}}$	$\varphi_{\text{ROT}}$
...	...	...	...	...	...
value	■■■■	■■■■	■■■■	■■■■	■■■■
value	■■■■	■■■■	■■■■	■■■■	■■■■
value	■■■■	■■■■	■■■■	■■■■	■■■■
...	...	...	...	...	...

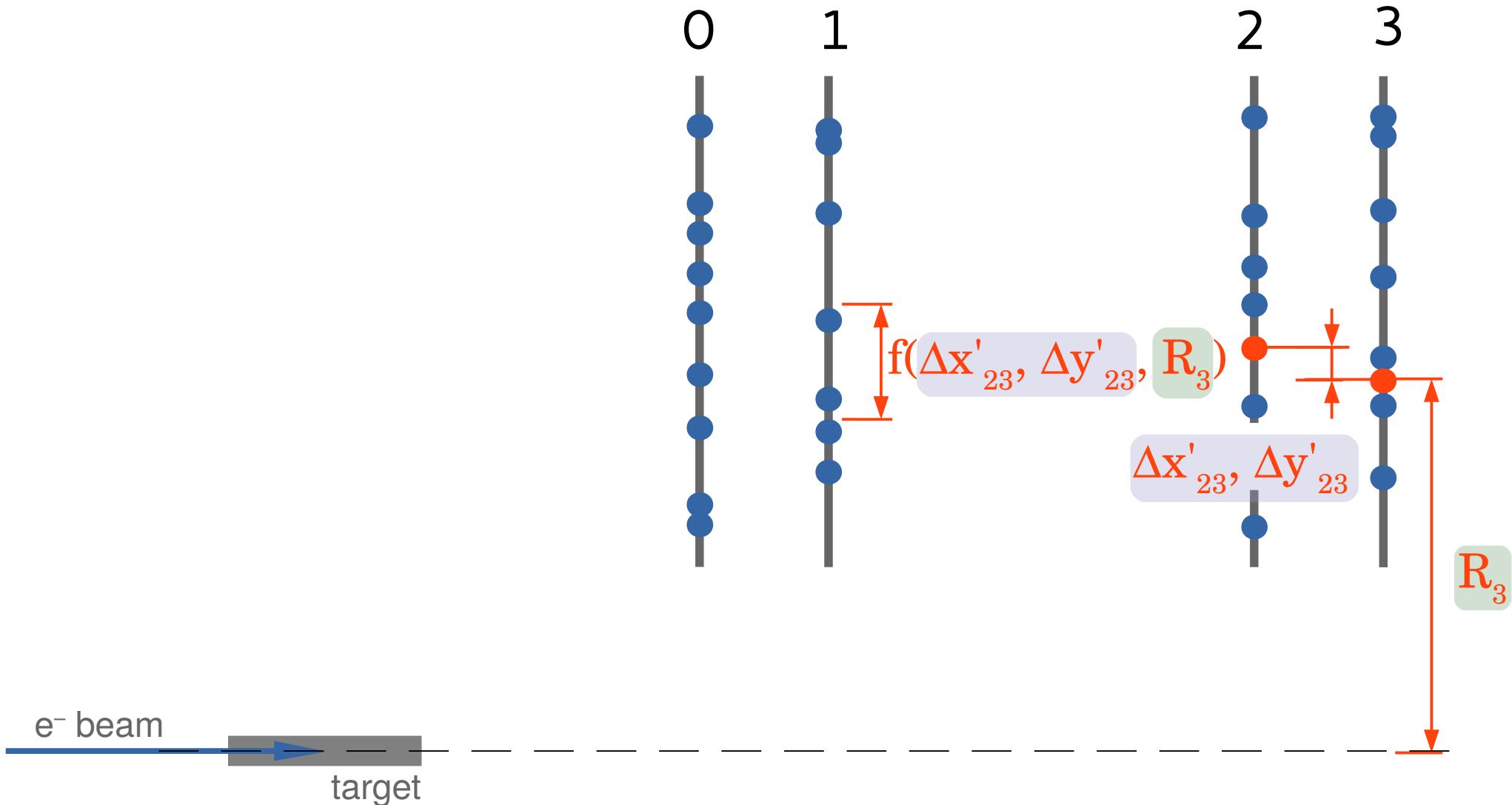


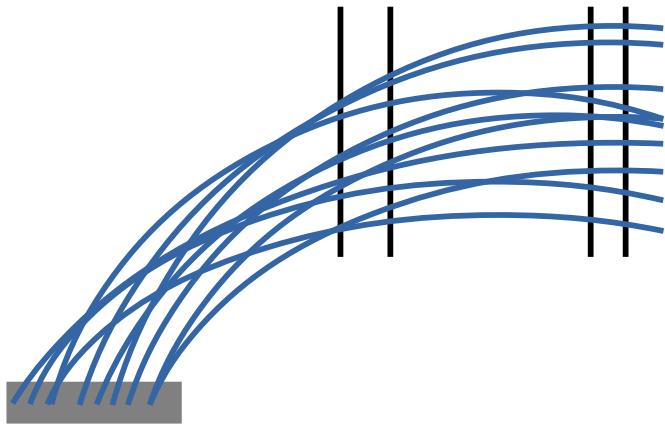
Fake plot.  
For illustration  
only.

# Search window for plane 2

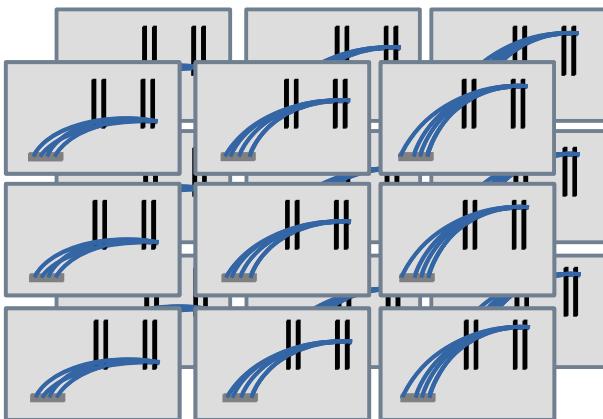


# Search window for plane 1





bin by  
 $\{R_3, \Delta x'_{23}, \Delta y'_{23}\}$



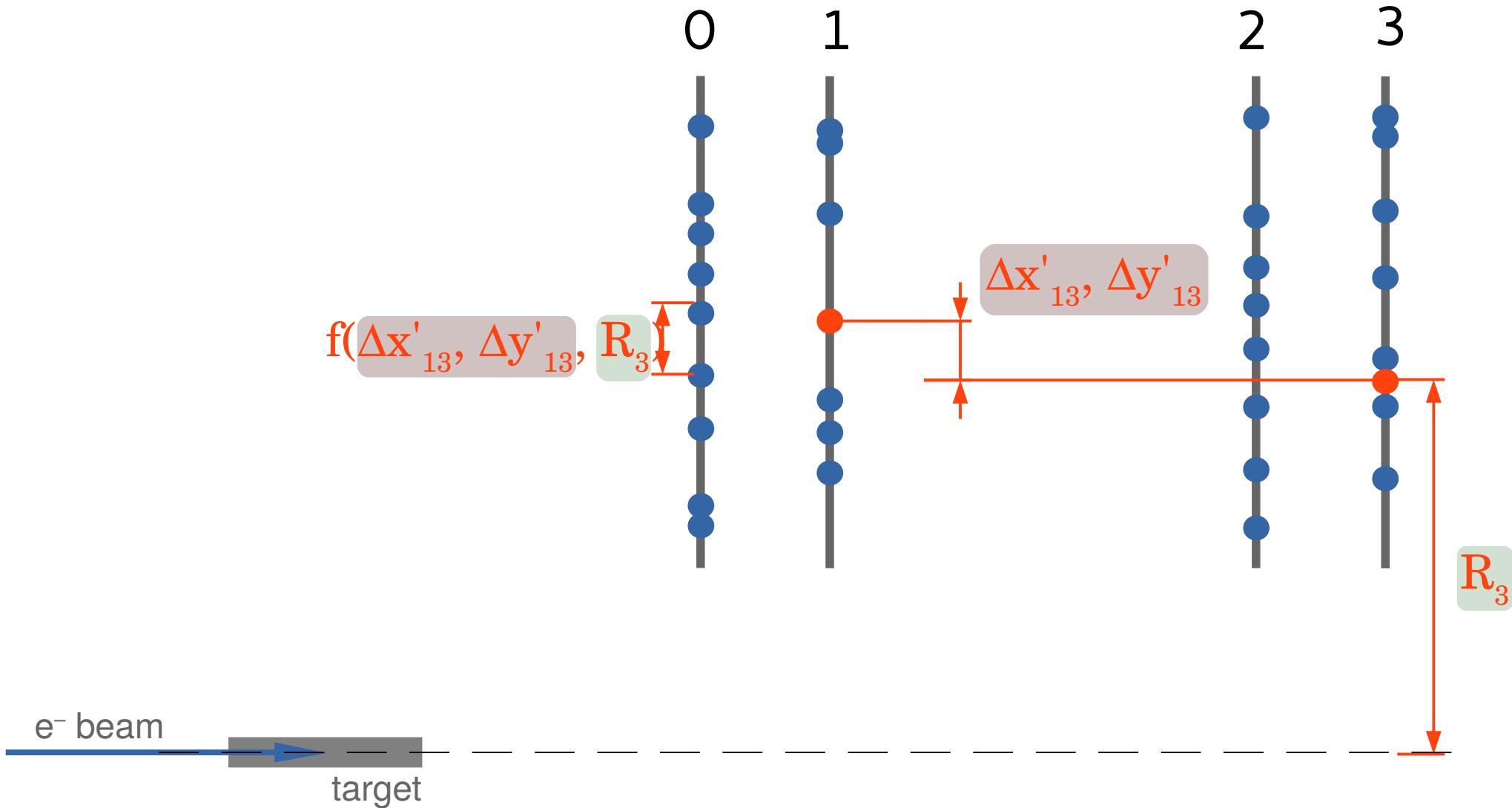
determine  
the search  
windows

$R_3$	$\Delta x'_{23}$	$\Delta y'_{23}$	$x_{\text{POS}}$	$y_{\text{POS}}$	$x_{\text{SIZE}}$	$y_{\text{SIZE}}$	$\varphi_{\text{ROT}}$
...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...

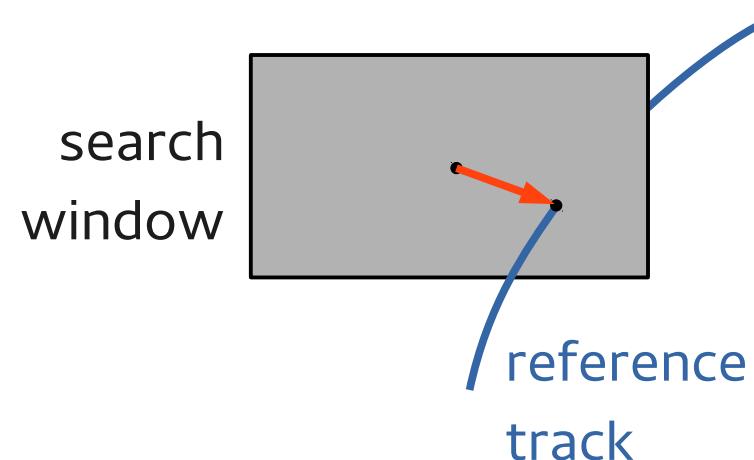
Fit (in 3D)

$$\begin{aligned}x_{\text{SIZE}} &= \text{pol3}( R_3, \Delta x'_{23}, \Delta y'_{23} ) \\y_{\text{SIZE}} &= \text{pol3}( R_3, \Delta x'_{23}, \Delta y'_{23} ) \\x_{\text{POS}} &= \text{pol3}( R_3, \Delta x'_{23}, \Delta y'_{23} ) \\y_{\text{POS}} &= \text{pol3}( R_3, \Delta x'_{23}, \Delta y'_{23} ) \\\varphi_{\text{ROT}} &= \text{pol3}( R_3, \Delta x'_{23}, \Delta y'_{23} )\end{aligned}$$

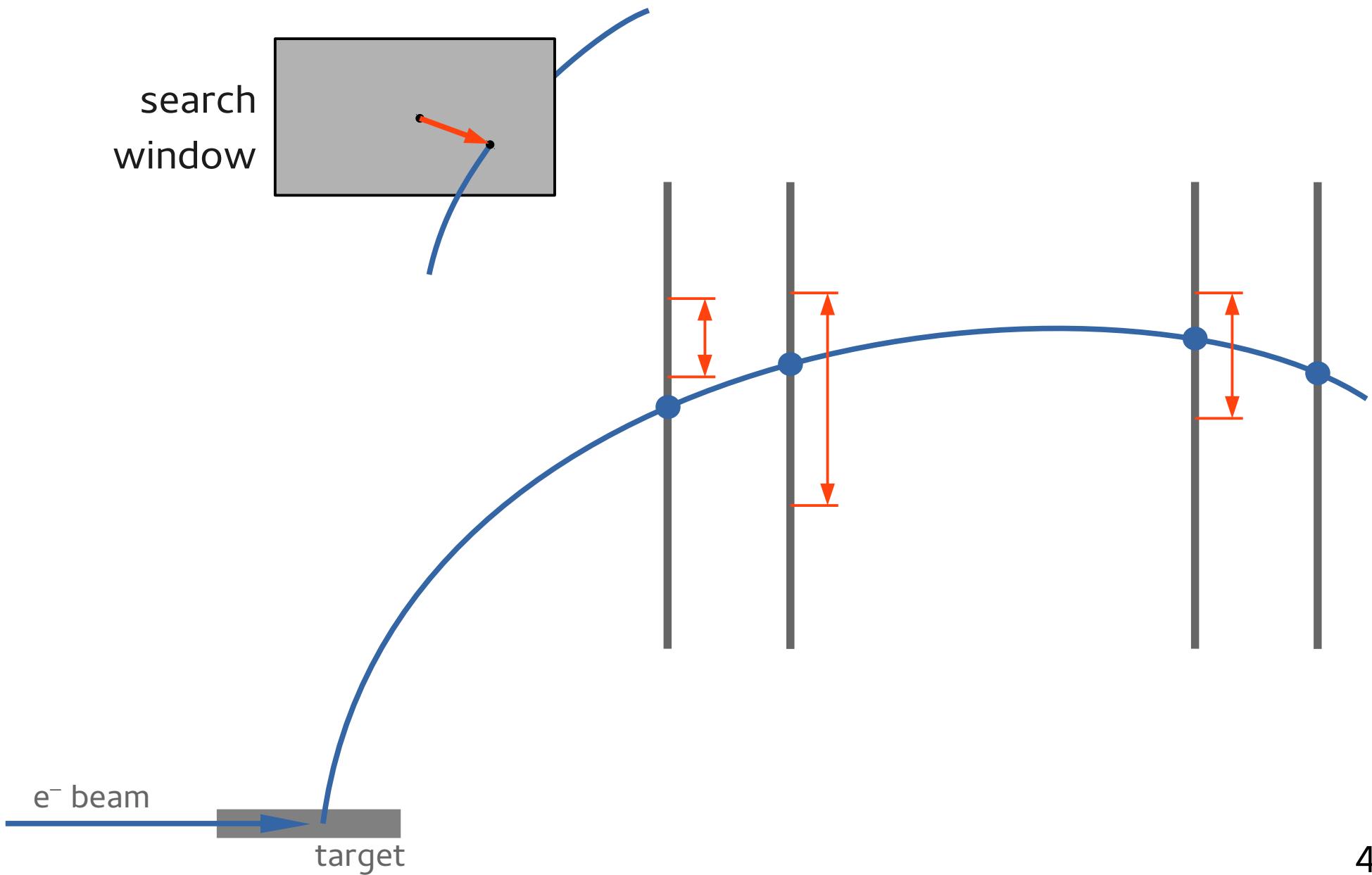
# Search window for plane 0



## Relative distance from the center of the search window

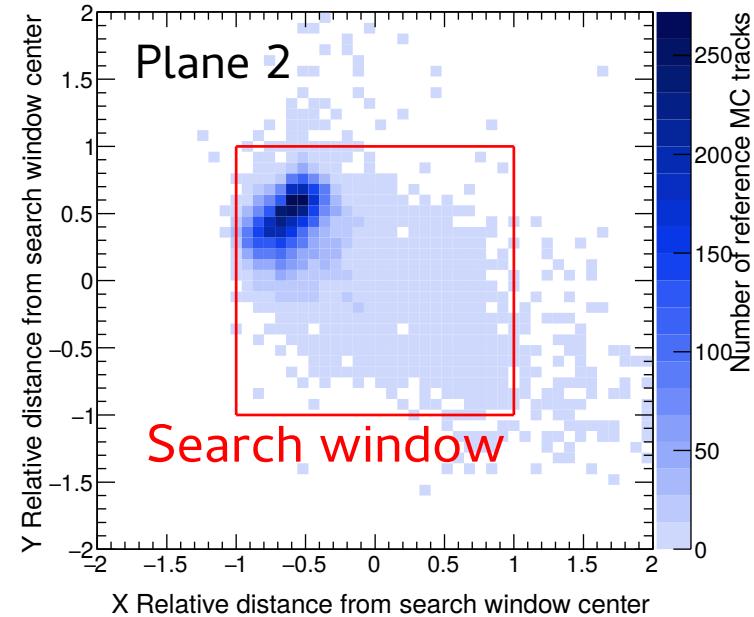
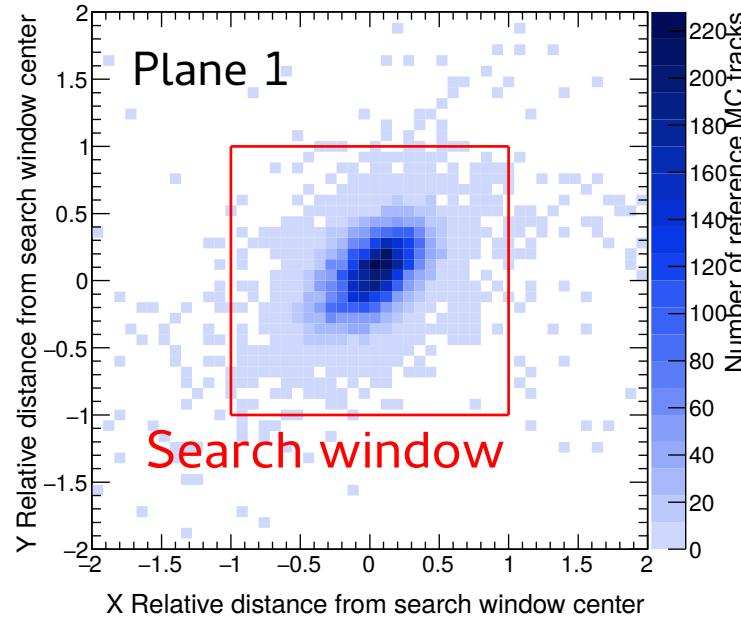
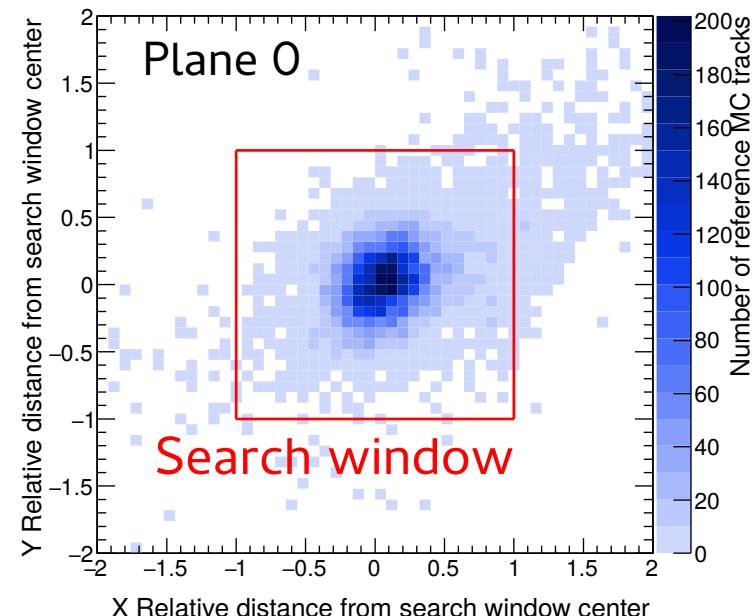
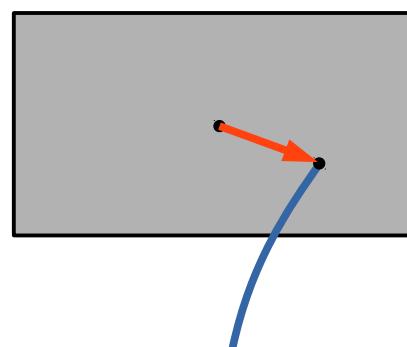


## Relative distance from the center of the search window



## Relative distance from the center of the search window

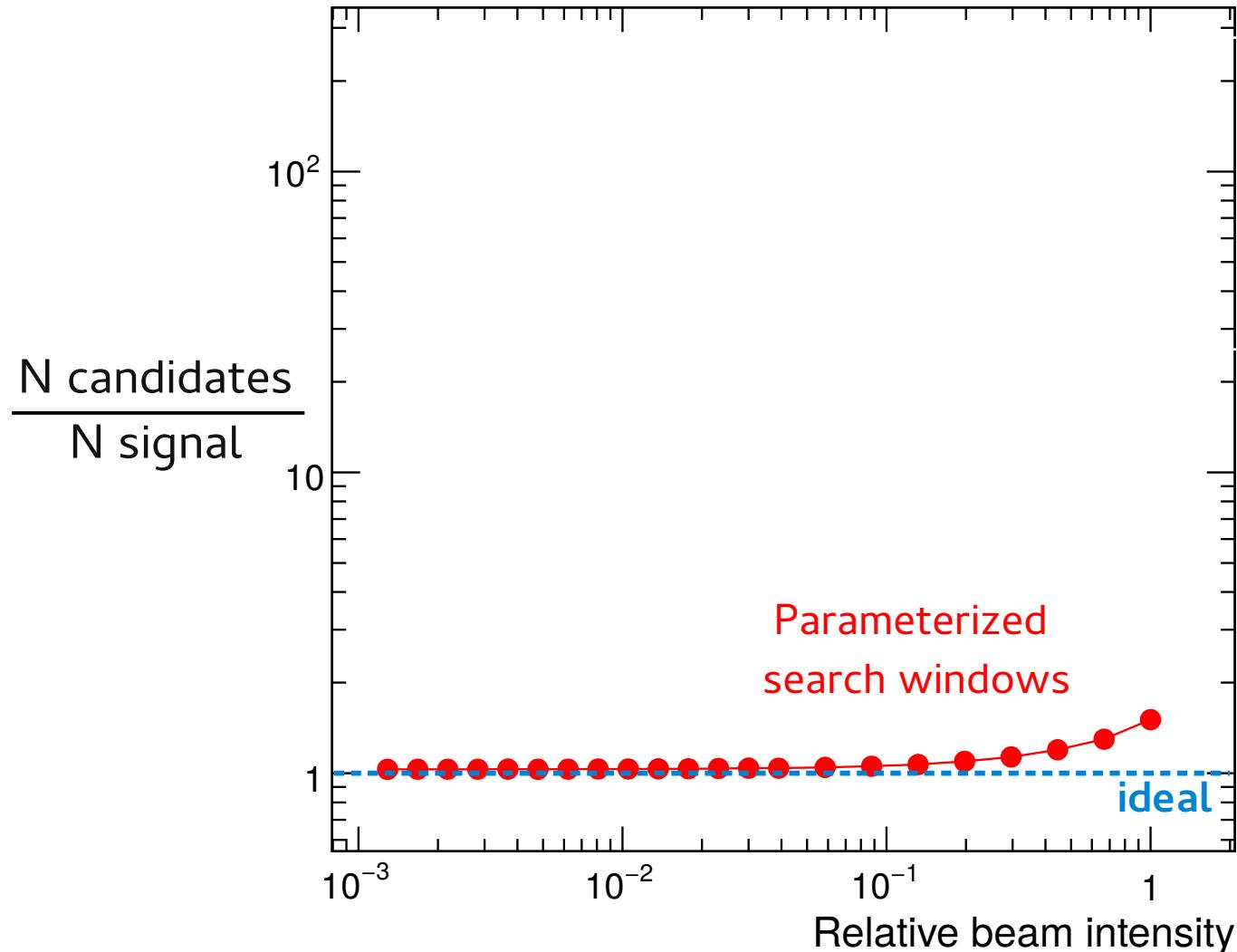
search  
window



Overall about 90% efficiency (depending on settings). 47

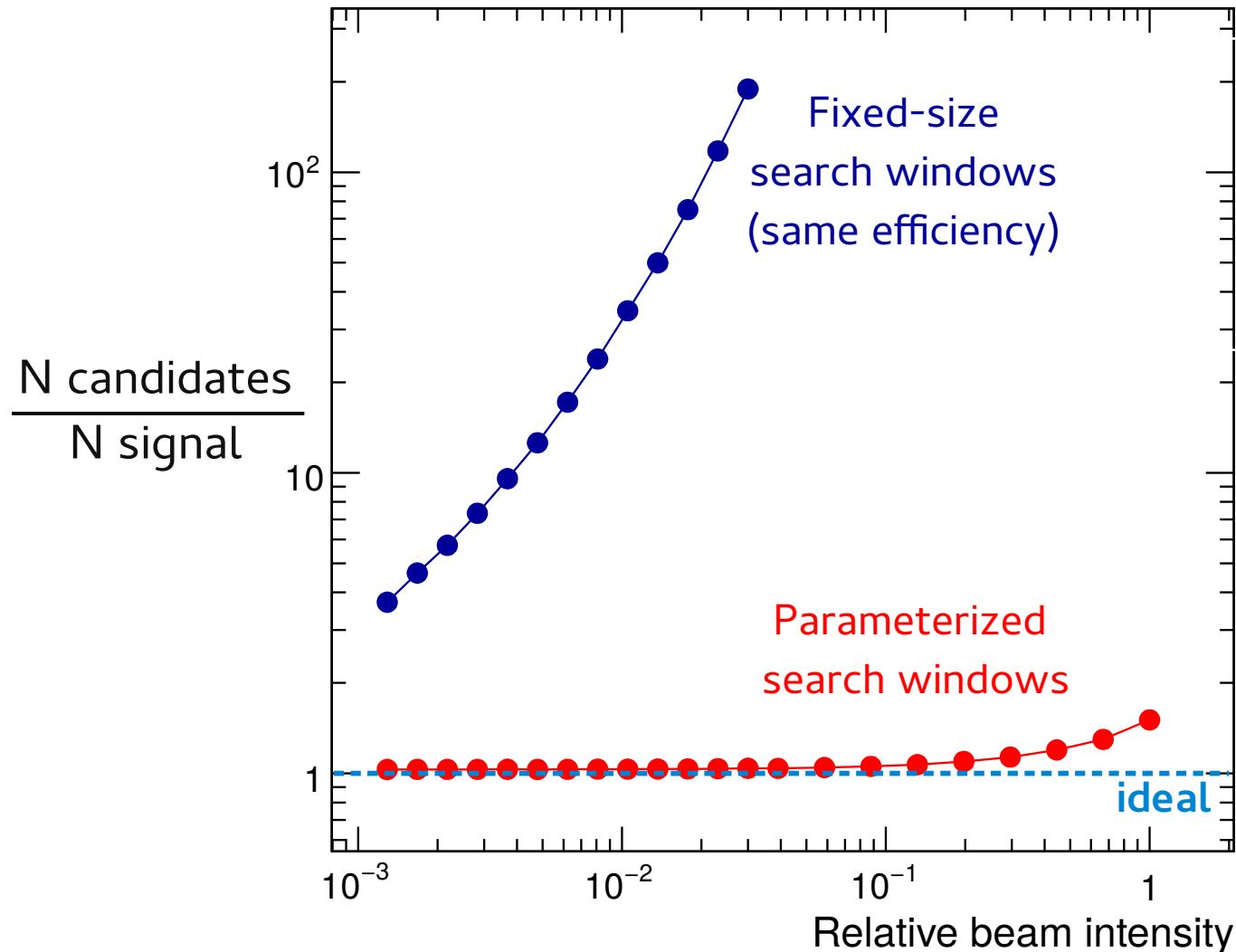
# Performance

Number of candidates per signal track



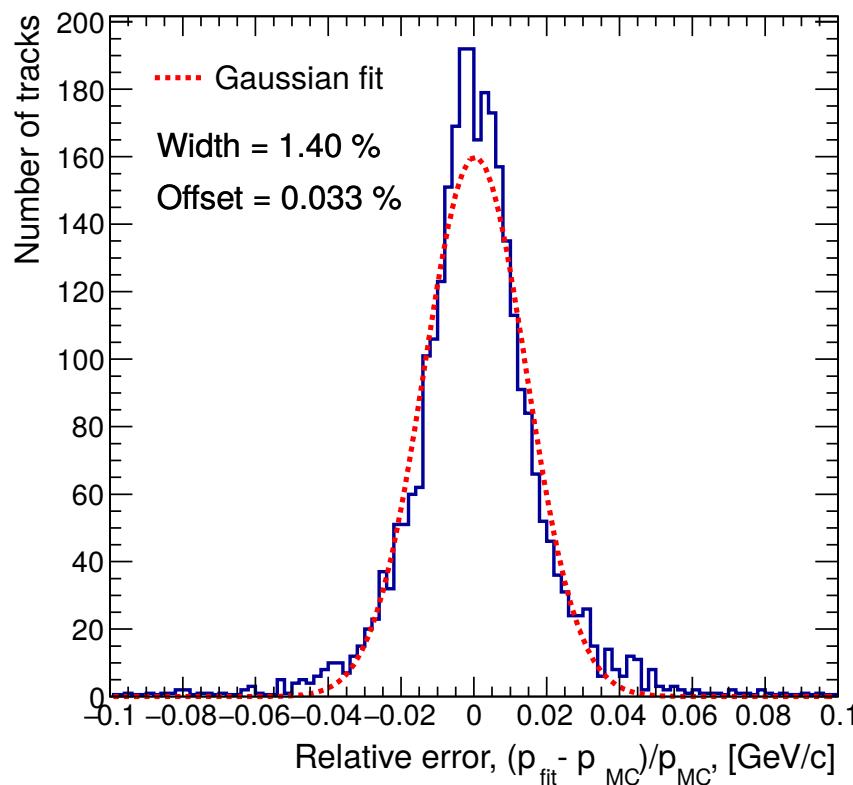
# Performance

Number of candidates per signal track

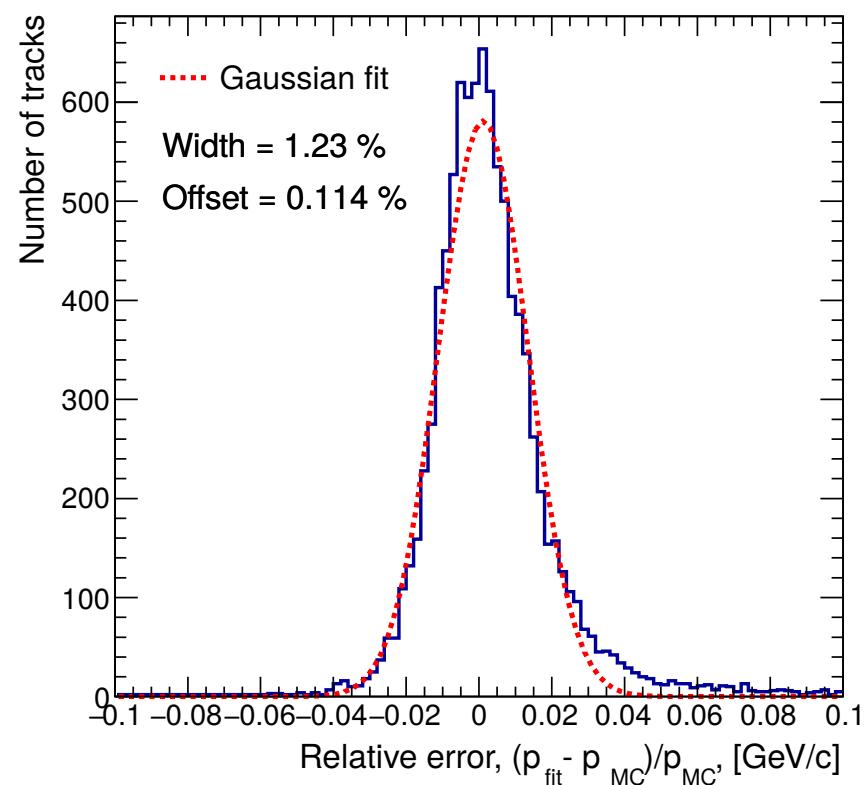


# Parameterization instead of fitting

Rigorous fit



Fit replaced by parameterization:  
momentum = pol3(  $R_3$ ,  $\Delta R_{31}$ ,  $\Delta \varphi_{31}$  )



Using GBL fit within the GENFIT framework

GBL: Kleinwort C. General Broken Lines as advanced track fitting method  
<http://dx.doi.org/10.1016/j.nima.2012.01.024>

GENFIT: Rauch J., Schlüter T. GENFIT – a Generic Track-Fitting Toolkit  
<https://doi.org/10.1088/1742-6596/608/1/012042>

# Summary

Parameterization-based tracking:

- replaces rigorous model calculations by simple analytical parametric functions
- parameters can be tuned based on real data or model (MC or deterministic with covariance)
- enables accurate, efficient, and very fast track finding
- can be used to estimate the kinematic parameters
- works well in P2 due to narrow momentum range